

# Design issues of “an anonymous authentication and key agreement protocol in smart living”

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**Abstract.** The Li et al.’s scheme [Computer Communications, 186 (2022), 110-120] uses XOR operation to realize the private transmission of sensitive information, under the assumption that if only one parameter in the expression  $a = b \oplus c$  is known, an adversary cannot retrieve the other two. The assumption neglects that the operands  $b$  and  $c$  must be of the same bit-length, which leads to the exposure of a substring in the longer operand. The scheme wrongly treats timestamps as random strings to encrypt a confidential parameter. These misuses result in the loss of sensor node’s anonymity, the loss of user anonymity and untraceability, insecurity against off-line password guessing attack, and insecurity against impersonation attack. The analysis techniques developed in this note is helpful for the future works on designing such schemes.

**Keywords:** Authentication; Anonymity; Key agreement; Impersonation attack

## 1 Introduction

A wireless sensor network (WSN) usually consists of tens to thousands of wireless sensor nodes that communicate through wireless channels for information sharing and cooperative processing [12]. It can be deployed on a global scale for environmental monitoring and habitat study, in factories for condition based maintenance, in buildings for infrastructure health monitoring, in homes to realize smart homes, in bodies for patient monitoring, etc [3, 11, 13]. A wireless sensor node consists of sensing, computing, communication, actuation, and power components [5]. These components are integrated on a single or multiple boards. The security and privacy of WSNs have gained much attention [1, 9]. In 2023, Tyagi and Kumar [14] presented a multi-factor user authentication and key agreement scheme for WSNs using Chinese remainder theorem. Darbandeh and Safkhani [6] proposed a secure authentication protocol for WSNs based on RFID tags. Khah et al. [7] suggested a dynamic and multi-level key management method for WSNs. Chen et al. [4] designed a provably-secure authenticated key agreement protocol for remote patient monitoring systems.

In 2022, Li et al. [8] proposed an anonymous authentication and key agreement protocol in smart living. The scheme uses only very low-cost bit-wise operation and hashing in order to realize the private transmission of sensitive information. The scheme treats timestamps as random strings to encrypt a confidential parameter, and also views a user’s identity as a random string. In this note, we show that the scheme has some design issues, including the loss of sensor node’s anonymity, the loss of user anonymity and untraceability, insecurity against off-line password guessing attack, and

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insecurity against impersonation attack. To the best of our knowledge, it is first time to develop these analysis techniques for such authentication and key agreement protocols.

## 2 Review of the Li et al.'s scheme

In the considered scenario, there are three parties: users, gateway, and sensor nodes. Let  $h(\cdot)$  be a hash function with the output length 256 bits. The scheme depends mainly on XOR encryption. The involved notations are listed below (Table 1). The scheme is designed to meet many security requirements, including users' anonymity and untraceability, sensor nodes' anonymity, forward security and backward security, resisting replay attack, stolen smart card attack, impersonation attack, off-line password guessing attack, and insider attack.

The administrator stores some fundamental operation functions in the memory of smart card  $SC$ , gateway node  $GWN$ , and sensor node  $N_j$ . Then, the administrator selects an identity  $ID_{SC}$  and a random number  $R_{SC}$  for the smart card  $SC$ , and stores  $\{ID_{SC}, R_{SC}\}$  to the user's authentication table and  $SC$ 's memory. The registration phase can be depicted as below (Table 2).

Table 1: Notations and descriptions

$GWN, X$	gateway node, and its master key
$U_i, ID_i$	the $i$ th user, and its identity
$N_j, ID_j$	the $j$ th sensor node, and its identity
$SC, ID_{SC}$	smart card, and its identity
$PW_i$	$U_i$ 's password
$TS_i$	time stamp
$\Delta T$	tolerable transmission delay
$\parallel$	concatenation operator
$\oplus$	XOR operator
$R_U, R_{GWN}, R_N, R_{SC}$	random number generated by user, gateway, sensor node, and smart card, respectively

Table 2: The user registration phase

$U_i: SC = \{ID_{SC}, R_{SC}, h(\cdot)\}$ Choose $ID_i, PW_i$ .		$GWN: X, h(\cdot), \{ID_{SC}, R_{SC}\}$
Pick a nonce $R_U$ .	$\xrightarrow[\text{[open channel]}]{ID_{SC}, RPW_i, REG_i}$	Check $\{ID_{SC}, R_{SC}\}$ . Generate
Compute $RPW_i = h(PW_i \parallel R_U)$ , $REG_i = ID_i \oplus h(R_{SC} \parallel RPW_i)$ .		the timestamp $TS_i$ . Compute $ID_i = REG_i \oplus h(R_{SC} \parallel RPW_i)$ , $US = h(ID_i \parallel X)$ , $SE = TS_i \oplus h(US \parallel ID_i)$ , $UR = US \oplus h(ID_i \parallel RPW_i)$ ,
Compute	$\xleftarrow{RSP_i}$	$UV = h(ID_i \parallel US \parallel RPW_i) \oplus TS_i$ ,
$(UR \parallel SE \parallel UV) = RSP_i \oplus h(ID_i \parallel R_{SC})$ , $RE = R_U \oplus h(ID_i \parallel PW_i)$ .		$RSP_i = h(ID_i \parallel R_{SC}) \oplus (UR \parallel SE \parallel UV)$ , $XT_i = h(X \parallel TS_i) \oplus ID_i$ .
Update $SC = \{UR, SE, UV, RE, h(\cdot)\}$ .		Store $\{XT_i, TS_i\}$ .

Table 3: The authentication and key agreement phase

$U_i$ knows $ID_i^*, PW_i^*$ and has $SC = \{SE, RE, UR, UV, h()\}$ .	$GWN$ knows the master key $X$ and $\{ID_j, SV_j\}, \{XT_i, TS_i\}$ .	$N_j$ knows $\{ID_j, SV_j\}$ .
Insert $SC$ into a terminal and input $ID_i^*, PW_i^*, ID_j$ . The card $SC$ computes $R_U^* = RE \oplus h(ID_i^*    PW_i^*)$ , $RPW_i^* = h(PW_i^*    R_U^*)$ , $US^* = UR \oplus h(ID_i^*    RPW_i^*)$ , $TS_i^* = SE \oplus h(US^*    ID_i^*)$ , $UV^* = h(ID_i^*    US^*    RPW_i^*) \oplus TS_i^*$ . Check $UV = UV^*$ . If true, then $ID_i^* = ID_i, PW_i^* = PW_i$ . Choose a new timestamp $T_1$ , compute $M_1 = (ID_j    R_U) \oplus h(US    ID_i    TS_i)$ , $M_2 = h(ID_i    TS_i    US    T_1    ID_j)$ . $\xrightarrow{M_1, M_2, T_1, TS_i}$	Check the timestamp. Retrieve $XT_i$ by using $TS_i$ . Compute $ID_i' = h(X    TS_i) \oplus XT_i$ , $US' = h(ID_i'    X)$ , $ID_j'    R_U' = M_1 \oplus h(US'    ID_i'    TS_i)$ , $M_2' = h(ID_i'    TS_i    US'    T_1    ID_j')$ . Check $M_2 = M_2'$ . If so, generate $TS_i^{new}, R_{GWN}, T_2$ . Retrieve $SV_j'$ by using $ID_j'$ . Compute $c = TS_i \oplus TS_i^{new}$ , $M_3 = (R_U'    R_{GWN}) \oplus h(SV_j')$ , $M_4 = h(ID_j'    R_{GWN}    T_2    SV_j')$ . $\xrightarrow{M_3, M_4, T_2}$	Check the timestamp. Compute $R_U''    R_{GWN}' = M_3 \oplus h(SV_j)$ , $M_4' = h(ID_j    R_{GWN}'    T_2    SV_j)$ . Check $M_4' = M_4$ . If so, generate $R_N, T_3$ , and compute $M_5 = R_N \oplus h(SV_j)$ , $SK = h(R_U''    R_{GWN}'    R_N)$ , $M_6 = h(SK    SV_j    R_N    T_3    ID_j)$ . $\xleftarrow{M_5, M_6, T_3}$
Check the timestamp. Compute $c' = M_7 \oplus US, TS_i^{new1} = c' \oplus TS_i$ , $R_{GWN}'    R_N'' = M_8 \oplus h(R_U    US)$ , $SK'' = h(R_U    R_{GWN}'    R_N'')$ , $M_9' = h(SK''    ID_i    TS_i^{new1}    US    T_4)$ . Check $M_9' = M_9$ . If so, generate a nonce $R_U^{new}$ , compute $SE^{new} = SE \oplus c'$ , $RE^{new} = RE \oplus R_U \oplus R_U^{new}$ , $RPW_i^{new} = h(PW_i    R_U^{new})$ , $UR^{new} = US \oplus h(ID_i    RPW_i^{new})$ , $UV^{new} = h(ID_i    US    RPW_i^{new}) \oplus TS_i^{new}$ . $SC = \{SE^{new}, RE^{new}, UR^{new}, UV^{new}, h()\}$ .	Check the timestamp. Compute $R_N' = M_5 \oplus h(SV_j)$ , $SK' = h(R_U'    R_{GWN}    R_N')$ , $M_6' = h(SK'    SV_j'    R_N'    T_3    ID_j')$ . Check $M_6' = M_6$ . If so, choose $T_4$ to compute $M_7 = c \oplus US'$ , $M_8 = (R_{GWN}    R_N') \oplus h(R_U'    US')$ , $M_9 = h(SK'    ID_i'    TS_i^{new}    US'    T_4)$ . $\xleftarrow{M_7, M_8, M_9, T_4}$	

### 3 The flaws in Li et al.'s scheme

Though the Li et al.'s authentication and key agreement scheme [8] is interesting, we find it has some flaws, including the misuse of XOR operation, the loss of sensor node's anonymity, the loss of user untraceability, insecurity against stolen smart card attack, insecurity against off-line password guessing attack, and insecurity against impersonation attack.

### 3.1 The misuse of XOR operation

The Boolean logic operation XOR, denoted by  $\oplus$ , is widely used in cryptography which compares two input bits and generates one output bit [10]. If the bits are the same, the result is 0. If the bits are different, the result is 1. When the operator is performed on two strings, they must be of the same bit-length. Otherwise, the shorter string is usually stretched by padding some 0s to its left side. In this case, the partial string corresponding to the padding bits is eventually exposed to the adversary.

In the user registration phase, it specifies that

$$\begin{aligned} \text{Encryption: } \underbrace{RSP_i}_{\text{ciphertext}} &= \underbrace{h(ID_i||R_{SC})}_{\text{secret key}} \oplus \underbrace{(UR||SE||UV)}_{\text{plaintext}} \\ \text{Decryption: } (UR||SE||UV) &= RSP_i \oplus h(ID_i||R_{SC}) \\ \text{where } UV &= h(ID_i||US||RPW_i) \oplus TS_i \end{aligned}$$

Actually, we have

$$\begin{aligned} RSP_i &= \underbrace{h(ID_i||R_{SC})}_{256 \text{ bits}} \oplus (UR||SE|| \underbrace{h(ID_i||US||RPW_i) \oplus TS_i}_{256 \text{ bits}}) \\ &= UR||SE|| \underbrace{(h(ID_i||R_{SC}) \oplus h(ID_i||US||RPW_i) \oplus TS_i)}_{256 \text{ bits}} \end{aligned}$$

That means the substring  $UR||SE$  is entirely copied into the resulting string  $RSP_i$ . The adversary who has eavesdropped on the open channel and obtained the string, can successfully retrieve the parameters  $UR, SE$ . The confidential parameters are eventually exposed.

### 3.2 The loss of sensor node's anonymity

As for the sensor node's anonymity, it argues that: “*In our protocol, the real identity  $ID_j$  of the sensor node does not explicitly exist in any communication messages, so the adversary cannot directly obtain the sensor's  $ID_j$  according to the communication messages on the public channel. Furthermore, the adversary cannot compute  $ID_j||R_U = M_1 \oplus h(US||ID_i||TS_i)$  without knowing  $US$  and the user's real identity  $ID_i$ .*” We find the argument is nor sound. Actually, in the authentication and key agreement phase, it specifies that

$$\begin{aligned} \text{Encryption: } \underbrace{M_1}_{\text{ciphertext}} &= \underbrace{(ID_j||R_U)}_{\text{plaintext}} \oplus \underbrace{h(US||ID_i||TS_i)}_{\text{nonce}}, \\ \text{Decryption: } ID_j||R_U &= M_1 \oplus h(US||ID_i||TS_i), \\ \text{where } R_U &= RE \oplus h(ID_i||PW_i). \end{aligned}$$

Hence, we have

$$\begin{aligned} M_1 &= (ID_j|| \underbrace{RE \oplus h(ID_i||PW_i)}_{256 \text{ bits}}) \oplus \underbrace{h(US||ID_i||TS_i)}_{256 \text{ bits}} \\ &= ID_j|| (RE \oplus h(ID_i||PW_i) \oplus h(US||ID_i||TS_i)) \end{aligned}$$

which means the sensor node’s identity  $ID_j$  is entirely copied into the string  $M_1$ . An adversary who has captured the data via the open channel, can easily recover the identity  $ID_j$ .

### 3.3 The loss of user untraceability

The user untraceability says that an adversary cannot trace a target user in different sessions. As for this property, it argues that: “*Since each user accesses the gateway irregularly and new users register to the gateway, there is no connection between the dynamic sequence  $TS_i$  used in this session and  $TS_i^{new}$  used in the next session. Besides, the communication messages  $\{M_1, M_2, T_1, TS_i\}$  are different since the user uses different random number  $R_U$  in each session.*” We find the argument is not sound. In fact,

$$c = TS_i \oplus TS_i^{new}, \quad US = h(ID_i \| X), \quad M_7 = c \oplus US$$

where  $ID_i$  is the user’s identity,  $X$  is the GWN’s master key. Note that *the timestamps  $TS_i$  and  $TS_i^{new}$  cannot be viewed as two random strings*, which are publicly available to any adversary. So, the adversary can obtain  $c$ . Using the captured  $M_7$  via the open channel, the adversary can obtain  $h(ID_i \| X) = US = c \oplus M_7$ . The hash value  $h(ID_i \| X)$  is invariable for different sessions for the same user, because the identity  $ID_i$  and the master key  $X$  are two long-term parameters in the proposed scheme. Although the adversary cannot recover the identity  $ID_i$  from the hash value  $h(ID_i \| X)$  due to its one-way property, he can trace a target user by checking the consistency of this hash value. In fact, for a different identity  $\widehat{ID}$ , the probability of event that  $h(ID_i \| X) = h(\widehat{ID} \| X)$  is negligible, due to the collision-free property of the hash function.

### 3.4 The loss of user anonymity

The user anonymity means that an adversary cannot obtain a user’s real identity. But we find the scheme fails to keep this property. In fact, the adversary can capture the parameters  $M_1, M_2, T_1, TS_i$  via the open channel. By the above analysis (see §3.2, §3.3), we know, the adversary can also recover  $ID_j$  and  $US$ .

In order to launch a session, the user  $ID_i$  needs to inquire about the target sensor node’s identity  $ID_j$ . If the identity  $ID_j$  is not publicly available, the user cannot complete the later procedure. We want to stress that a user’s identity is the characteristics that *distinguish* it from others. So, it is publicly available for the purpose of distinguishing members, not a confidential parameter [2].

Let  $\Upsilon$  be the set of all identities in the system. Since  $M_2 = h(ID_i \| TS_i \| US \| T_1 \| ID_j)$ , the adversary can test the following equation

$$M_2 = h(\psi \| TS_i \| US \| T_1 \| ID_j), \quad \forall \psi \in \Upsilon \tag{1}$$

to determine which  $\psi$  is the target identity. Practically, the size of  $\Upsilon$  is moderate, and the success probability of this exhaust search attack is not negligible. All in all, the scheme [8] has falsely treated the identity  $ID_i$  as a random string.

### 3.5 Insecurity against off-line password guessing attack

When an adversary gets a legitimate user’s smart card  $SC = \{SE, RE, UR, UV\}$ , he acquires the parameters stored in it. In this case, the adversary can launch the off-line password guessing attack.

Concretely, he first recovers the user’s identity  $ID_i$  and the parameter  $US$  by the above analysis (see §3.4). He then makes use of the following relations

$$\begin{aligned} R_U &= RE \oplus h(ID_i \| PW_i), \\ RPW_i &= h(PW_i \| R_U), \\ US &= UR \oplus h(ID_i \| RPW_i), \end{aligned}$$

to construct the challenging equation

$$US = UR \oplus h(ID_i \| h(\phi \| RE \oplus h(ID_i \| \phi))), \forall \phi \in \Phi \tag{2}$$

where  $US, UR, ID_i, RE$  have been recovered, and  $\Phi$  is the given password dictionary. Once a password satisfies the Eq.(2), the original password or an equivalent password is searched out.

### 3.6 Insecurity against impersonation attack

By the sections §3.4 and §3.5, we know, an adversary who has captured the smart card  $SC$  can recover the target user’s identity  $ID_i$  and password  $PW_i$ . Having the two confidential parameters, the adversary can impersonate the user to start other sessions. Therefore, the scheme is insecure against impersonation attack.

## 4 Conclusion

We show that the Li et al.’s authentication and key agreement scheme has some flaws. It seems difficult to fix the scheme because of its simple encryption mechanism. The findings in this note could be helpful for the future work on designing such schemes.

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