LMS-SM3 and HSS-SM3: Instantiating Hash-based Post-Quantum Signature Schemes with SM3

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Abstract. We instantiate the hash-based post-quantum *stateful* signature schemes LMS and HSS described in RFC 8554 and NIST SP 800-208 with SM3, and report on the results of the preliminary performance test.

Keywords: Hash Functions, Digital Signatures, Leighton-Micali Signature, Hierarchical Signature System, SM3

1 Introduction

It is well known that the security of many widely deployed digital signature schemes (e.g., RSA, DSA, and ECDSA) will be compromised if large-scale quantum computers are ever built [Sho99]. Hash-based signature scheme is one important type of quantum-resistant cryptographic algorithms. Generally speaking, there are two approaches for constructing signature schemes based on hash functions. The first one signs messages by exposing the pre-images of certain one-way functions [Lam79, Mer89, BDH11], the second one signs message by proving the possession of the pre-images with zero-knowledge techniques [CDG+17]. In this work, we restrict our attention to the former approach. Also, we only consider hash-based stateful signature schemes, since these type of hash-based signature schemes are actively standardized [MCF19, HBG+18, NIS20] and are more appealing with regards to performance and resource consumption. For the construction of stateless hash-based signature schemes, we refer the reader to [BHH+15, BHK+19] for more information.

The study of hash-based signature schemes has a long history. The first such scheme can be traced back to 1976 [DH76], where Diffie and Hellman proposed a one-time signature scheme for signing a single bit. After more than 40 years of development, the construction and implementation of hash-based signatures are well studied and have benefited from renewed attention in the last decade due to the concern of quantum attacks.

Hash-based stateful signatures have the following advantages. Firstly, hash-based signatures are arguably the most conservative designs with respect to

security. They enjoy provable security which relies so solely on the (second) pre-image resistance of the underlying hash functions secondly, They are hash-function-agnostic, meaning that any compatible hash function can be used to instantiate the schemes. Therefore, when one hash function is insecure, we can simply replace it with a secure one. Thirdly, it features small private and public keys, and fast signature generation and verification, making it suitable for compact verifier implementations. Finally, hash-based signatures have a rich set of tunable parameters, and thus it is easy to tailor the designs for specific application scenarios [WJW+19, HRB17, vdLPR+18, ZCY22]. The disadvantage of stateful hash based signatures including large signature sizes, and the issue of state management.

Outline. In section 2 we give some preliminaries and notations used later. Section 3 describes the one-time signature scheme LM-OTS which is employed as a building block for the many-time signature schemes LMS and HSS introduced in Section 4 and Section 5, respectively. In Section 6, we instantiate these hash-based signature schemes with SM3 and report on the results of the performance test on some preliminary implementations without optimization.

2 Notations and Preliminaries

Let $\mathbb{F}_2 = \{0,1\}$ be the binary field and $\mathbb{B} = \mathbb{F}_2^8$ be the set of all 8-bit binary strings. Concrete values of byte strings are specified in binary or hexadecimal notations. For example, we use 0x1F12 to denote the 2-byte string (0001 1111 0001 0010)₂. Sometimes, we need to convert a unsigned integer into a string of bytes, which is done by applying the conversion functions $u8str(\cdot)$, $u16str(\cdot)$, and $u32str(\cdot)$. For example, u8str(11) = 0x0B, u16str(6214) = 0xF2BC, and u32str(305441741) = 0x1234ABCD. Conversely, we use $int32(\cdot)$ to convert an integer $i \in \{0, 1, \dots, 2^{32} - 1\}$ to a 4-byte string. For example, int32(0x1234ABCD) = 305441741. Also, u32str(int32(S)) = S holds for any 4-byte string S.

Let S be a byte string. Then, byte(S,i) denotes the i-th byte of S, and byte(S,i,j) denotes the range of bytes from the i-th to the j-th byte, inclusive. For example, if S = OxABCDFFO1, then byte(S,0) = OxAB, byte(S,3) = OxO1, and byte(S,1,3) = OxCDEFO1. In addition, for $w \in \{1,2,4,8\}$, we use coef(S,i,w) to denote the unsigned integer represented by the i-th w-bit string of S. For example, S = OxABCDFFO1, then coef(S,0,4) = OxA = 10, coef(S,6,4) = 0x0 = 0, and coef(S,3,2) = 3. Also, we always have coef(S,i,8) = byte(S,i).

3 The Leighton-Micali One-Time Signature (LM-OTS)

LM-OTS is a ote-time signature scheme, meaning that each private key must be used at most one time to sign any given message. Otherwise, the security of the signature scheme is not guaranteed. In the sequel, an LM-OTS private and public

key pair is referred to as an LM-OTS instance. Therefore, to generate an LM-OTS instance is to generate an LM-OTS key pair.

Before key generation, three system parameters must be determined, including the employed hash function $H(\cdot)$, the number of bytes of the output of the hash function, denoted by n, and the Winternitz parameter $w \in \{1, 2, 4, 8\}$.

3.1 LM-OTS Private Key Generation

First, set the 4-byte value of of the according to Table 1, which is compatible with RFC 8554 [MCF19] and the Internet draft [FD22] work in progress. If we instantiate the LM-OTS scheme with SM3, the value of of the set according to Table 3 in this article. Then, set I to be a randomly chosen 16-byte string. Next, we set q=0.

Then, we need to generate $x=(x[0],\cdots,x[p-1])\in\mathbb{B}^{np}$, where x[j] is an n-byte string for $0\leq j< p$. We call x the array of secret pre-images of the LM-OTS secret key. The number p of pre-images in the array is determined by n and $w\in\{1,2,4,8\}$, and can be computed as p=u+v with

$$\begin{cases} u = \frac{8n}{w} \\ v = \left\lceil \frac{\lfloor \log_2(u(2^w - 1)) \rfloor + 1}{w} \right\rceil \end{cases} , \tag{1}$$

where u is the number of w-bit fields needed to hold the n-byte output of the hash function and v is the number of w-bit fields needed to hold the checksum described in Section 3.3.

To generate the array x, there are two methods. In the first method, we can just independently set x[j] to be a uniformly random n-byte string for each $j \in \{0, \dots, p-1\}$. In the second method, we can generate x[j] pseudorandomly from a secret seed SEED $\in \mathbb{B}^n$ such that

$$x[j] = H(I||u32str(q)||u16str(j)||0xFF||SEED)$$

for $j \in \{0, \dots, p-1\}$. The private key of the generated LM-OTS instance is $\mathsf{sk} = (\mathsf{otstype}, I, q, x) \in \mathbb{B}^4 \times \mathbb{B}^{16} \times \mathbb{B}^4 \times \mathbb{B}^{np}$, where $(\mathsf{otstype}, I, q)$ can be published and x must be kept secret.

In the following, we will use sk.FieldName to access a particular field of the given private key sk. For example, if

Then sk.otstype = 0x00000003.

3.2 LM-OTS Public Key Generation

From the LM-OTS secret key (otstype, I, q, x) with $x = (x[0], \dots, x[p])$ we can compute the LM-OTS public key pk = (otstype, I, q, K) = GenPubKey(otstype, I, q, x) with Algorithm 1, where the values of $\gamma_{n,w}$ is given in Table 4 for different n and w. Similarly, we will use pk.FieldName to access a particular field of the given public key pk.

Table 1: Values for ${\tt otstype}$ from RFC 8554

otstype name	H	n	w	otstype value
Reserved	_	-	_	0x0000000
LMOTS_SHA256_N32_W1	SHA256	32	1	0x0000001
LMOTS_SHA256_N32_W2	SHA256	32	2	0x0000002
LMOTS_SHA256_N32_W4	SHA256	32	4	0x0000003
LMOTS_SHA256_N32_W8	SHA256	32	8	0x0000004
Unassigned	_	_	_	$\mathtt{0x00000005} - \mathtt{0xDDDDDDDC}$
Reserved for private use	_	-	_	${\tt OxDDDDDDDDD}-{\tt OxFFFFFFF}$

Table 2: Additional values for otstype from the Internet draft [FD22]

		<i>J</i> 1		L
otstype name	H	n	w	otstype value
LMOTS_SHA256_N24_W1	SHA256-192	24	1	0x0000005
LMOTS_SHA256_N24_W2	SHA256-192	24	2	0x00000006
LMOTS_SHA256_N24_W4	SHA256-192	24	4	0x0000007
${\tt LMOTS_SHA256_N24_W8}$	SHA256-192	24	8	80000000x0
LMOTS_SHAKE_N32_W1	SHAKE256-256	32	1	0x0000009
LMOTS_SHAKE_N32_W2	SHAKE256-256	32	2	A000000x0
LMOTS_SHAKE_N32_W4	SHAKE256-256	32	4	0x000000B
LMOTS_SHAKE_N32_W8	SHAKE256-256	32	8	0x000000C
LMOTS_SHAKE_N24_W1	SHAKE256-192	24	1	0x000000D
LMOTS_SHAKE_N24_W2	SHAKE256-192	24	2	0x000000E
LMOTS_SHAKE_N24_W4	SHAKE256-192	24	4	0x000000F
LMOTS_SHAKE_N24_W8	SHAKE256-192	24	8	0x0000010

Table 3: Values of ${\tt otstype}$ for LM-OTS instantiated with SM3

	<u> </u>			
otstype name	H	n	w	otstype value
LMOTS_SM3_N32_W1	SM3	24	1	0x00000011
LMOTS_SM3_N32_W2	SM3	24	2	0x00000012
LMOTS_SM3_N32_W4	SM3	24	4	0x00000013
LMOTS_SM3_N32_W8	SM3	24	8	0x00000014

Table 4: The left shift offset $\gamma_{n,w}$

n	w	$\gamma_{n,w}$
32	1	7
32	2	6
32	4	4
32	8	0

Algorithm 1: $GenPubKey(\cdot)$: Compute the LM-OTS public key from the secret key

Input: The LM-OTS private key (otstype, I, q, x) $\in \mathbb{B}^4 \times \mathbb{B}^{16} \times \mathbb{B}^4 \times \mathbb{B}^{np}$ Output: The LM-OTS public key (otstype, I, q, K) $\in \mathbb{B}^4 \times \mathbb{B}^{16} \times \mathbb{B}^4 \times \mathbb{B}^n$ 1 for $0 \le i < p$ do $tmp \leftarrow x[i]$ for $0 \le j < 2^w - 1$ do $\mid tmp \leftarrow H(I \mid\mid \mathtt{u32str}(q) \mid\mid \mathtt{u16str}(i) \mid\mid \mathtt{u8str}(j) \mid\mid tmp)$ $y[i] \leftarrow tmp$ 6 $K \leftarrow H(I \parallel u32str(q) \parallel 0x8080 \parallel y[0] \parallel \cdots \parallel y[p-1])$ 7 Return (otstype, I, q, K)

LM-OTS Signature Generation

In the signature generation process, we need to employ the following $Cksm(\cdot)$ function described in Algorithm 2 as a subroutine. The signature

$$\sigma = \mathtt{otstype} \|C\|y[0]\| \cdots \|y[p-1] \in \mathbb{B}^4 \times \mathbb{B}^n \times \mathbb{B}^{np}$$

of a message $M \in \mathbb{F}_2^*$ can be computed by the Algorithm 3 with the secret key (otstype, I, q, x).

Algorithm 2: $Cksm_{n,w}(\cdot)$: Compute the checksum of an *n*-byte string

Input: An n-byte string S

Output: A 16-bit unsigned integer

- $\mathbf{1} \ sum \leftarrow 0$ $\begin{array}{ll} \mathbf{2} \ \ \mathbf{for} \ 0 \leq i < \frac{8n}{w} \ \ \mathbf{do} \\ \mathbf{3} \ \ \ \middle| \ \ sum \leftarrow sum + (2^w - 1) - \mathsf{coef}(S, i, w) \end{array}$
- 4 Return $sum \ll \gamma_{n,w}$

3.4LM-OTS Signature Verification

Given a message $M \in \mathbb{F}_2^*$ and its LM-OTS signature σ , σ can be verified with Algorithm 4. Note that according to Algorithm 4, a hypothetical public key can be computed from the LM-OTS signature.

The LMS Signature Scheme

Basically, the LMS signature scheme provides a method for organizing a set of 2^h LM-OTS instances in a perfect binary tree with height h such that each leaf

Algorithm 3: LMOTS_GenSig(\cdot): Compute the LM-OTS signature

```
Input: The message M \in \mathbb{F}_2^* and the private key \mathsf{sk} = (\mathsf{otstype}, I, q, x) Output: The LM-OTS signature of M

1 C \leftarrow \mathsf{A} random n-byte string

2 Q \leftarrow H(I \| \mathsf{u32str}(q) \| \mathsf{0x8181} \| C \| M)

3 Q \leftarrow Q \| \mathsf{Cksm}_{n,w}(Q)

4 \mathsf{for} \ 0 \leq i 

5 <math>a \leftarrow \mathsf{coef}(Q, i, w)

6 tmp \leftarrow x[i]

7 \mathsf{for} \ 0 \leq j < a \ \mathsf{do}

8 tmp \leftarrow H(I \| \mathsf{u32str}(q) \| \mathsf{u16str}(i) \| \mathsf{u8str}(j) \| tmp)

9 y[i] \leftarrow tmp

10 Return \mathsf{otstype} \| C \| y[0] \| \cdots \| y[p-1]
```

node is associated with an LM-OTS instance, and the root node is employed to authenticate the LM-OTS instances. We call this structure a Merkle tree or LMS tree, which corresponds to an LMS instances. The LMS instance can sign at most 2^h times in its life cycle, and each time a new signature is generated, one LM-OTS instance is consumed. Moreover, these LM-OTS instances are consumed in order. Figure 1 depicts an LMS tree with height 3, and the LM-OTS instances are consumed in the order: $T[8], T[9], \dots, T[15]$.

Before key generation, four system parameters must be determined, including the employed hash function $H(\cdot)$, the number m of bytes associated with each node of the underlying LMS tree, the height of the tree, and the otstype of the underlying LM-OTS scheme employed.

4.1 LMS Private Key Generation

First, set the 4-byte value 1mstype according to Table 5 and Table 6. If we instantiate the LMS scheme with SM3, the value of 1mstype can be set according to Table 7. Then, set the 4-byte value otstype as described in Section 3. Then, set I to be a randomly chosen 16-byte string. Then, we set I to be a randomly chosen 16-byte string.

Next, we need to generate 2^h LM-OTS arrays x_0, \cdots, x_{2^h-1} of secret pre-images with $x_i = (x_i[0], \cdots, x_i[p-1]) \in \mathbb{B}^{mp}$. There are two methods for generating these arrays. In the first method, we can just independently set x_j to be a uniformly random mp-byte string for each $i \in \{0, \cdots, 2^h-1\}$. In the second method, we can generate $x_i[j]$ pseudorandomly from a secret seed SEED $\in \mathbb{B}^m$ such that $x_i[j] = H(I| \text{u32str}(i)| \text{u16str}(j)| \text{0xFF}| \text{SEED})$ for $j \in \{0, \cdots, p-1\}$. Let $\mathbf{x} = (x_0, \cdots, x_{2^h-1})$, the LMS secret key is

$$(\mathtt{lmstype},\mathtt{otstype},I,q,\mathbf{x})\in\mathbb{B}^4 imes\mathbb{B}^4 imes\mathbb{B}^{16} imes\mathbb{B}^4 imes\mathbb{B}^{(2^h-1)mp}$$

$\textbf{Algorithm 4: LMOTS_VerifySig}(\cdot) : Verify \ the \ \texttt{LM-OTS} \ signature$

```
Input: The message M \in \mathbb{F}_2^*, signature \sigma, and public key
               pk = (otstype, I, q, K)
    Output: True is the signature is valid
 1 Determine n, I, q, p and K from the public key
 2 if byte(\sigma,0,3) \neq \mathsf{pk.otstype} then
 3 | Return INVALID
 4 if \sigma is not 4 + n(p+1)-byte long then
 5 Return INVALID
 6 C \leftarrow \texttt{byte}(\sigma, 4, 4 + n - 1)
 \mathbf{7}\ y[0] \leftarrow \mathtt{byte}(\sigma, 4+n, 4+2n-1)
 \mathbf{9} \ y[p-1] \leftarrow \mathtt{byte}(\sigma, 4+pn, 4+(p+1)n-1)
10 /* Compute the hypothetical public key K^\prime */
11 Q \leftarrow H(I||\mathbf{u32str}(q)||\mathbf{0x8181}||C||M)
12 Q \leftarrow Q \| \mathtt{Cksm}_{n,w}(Q) \|
13 for 0 \le i 
        a \leftarrow \mathtt{coef}(Q, i, w)
14
15
         tmp \leftarrow y[i]
         for a \le j < 2^w - 1 do
16
          | tmp \leftarrow H(I | \texttt{u32str}(q) | \texttt{u16str}(i) | \texttt{u8str}(j) | tmp) 
17
18
       z[i] \leftarrow tmp
19 K' = \leftarrow H(I \parallel \mathtt{u32str}(q) \parallel \mathtt{0x8080} \parallel z[0] \parallel \cdots \parallel z[p-1])
20 if pk.K = K' then
     Return TRUE
21
22 else
23 Return INVALID
```

Table 5: The values for ${\tt lmstype}$ from RFC 8554

			-	
lmstype name	H	m	h	lmstype value
Reserved	_	_	_	0x00000000 - 0x00000004
LMS_SHA256_M32_H5	SHA256	32	1	0x0000005
LMS_SHA256_M32_H10	SHA256	32	2	0x0000006
LMS_SHA256_M32_H15	SHA256	32	4	0x0000007
LMS_SHA256_M32_H20	SHA256	32	8	80000000x0
LMS_SHA256_M32_H25	SHA256	32	8	0x0000009
Unassigned	_	-	_	${\tt 0x0000000A-0xDDDDDDC}$
Reserved for private use	_	_	_	${\tt OxDDDDDDDD}-{\tt OxFFFFFFF}$

Table 6: The values for lmstype from the Internet draft [FD22]

lmstype name	H	m	h	<pre>lmstype value</pre>
LMS_SHA256_M24_H5	SHA256-192	24	5	A000000x0
LMS_SHA256_M24_H10	SHA256-192	24	10	0x000000B
LMS_SHA256_M24_H15	SHA256-192	24	15	0x000000C
LMS_SHA256_M24_H20	SHA256-192	24	20	0x000000D
LMS_SHA256_M24_H25	SHA256-192	24	25	0x000000E
LMS_SHAKE_M32_H5	SHAKE256-256	32	5	0x000000F
LMS_SHAKE_M32_H10	SHAKE256-256	32	10	0x0000010
LMS_SHAKE_M32_H15	SHAKE256-256	32	15	0x0000011
LMS_SHAKE_M32_H20	SHAKE256-256	32	20	0x0000012
LMS_SHAKE_M32_H25	SHAKE256-256	32	25	0x00000013
LMS_SHAKE_M24_H5	SHAKE256-192	24	5	0x0000014
LMS_SHAKE_M24_H10	SHAKE256-192	24	10	0x0000015
LMS_SHAKE_M24_H15	SHAKE256-192	24	15	0x0000016
LMS_SHAKE_M24_H20	SHAKE256-192	24	20	0x0000017
LMS_SHAKE_M24_H25	SHAKE256-192	24	25	0x00000018

Table 7: The values of lmstype for LMS instantiated with SM3

lmstype name	H	m	h	<pre>lmstype value</pre>
LMS_SM3_M32_H5	SM3	32	5	0x0000019
LMS_SM3_M32_H10	SM3	32	10	0x000001A
LMS_SM3_M32_H15	SM3	32	15	0x000001B
LMS_SM3_M32_H20	SM3	32	20	0x000001C
LMS_SM3_M32_H25	SM3	32	25	0x000001D

4.2 LMS Public Key Generation

Given the secret key (lmstype, otstype, I,q,\mathbf{x}), one can derive 2^h LM-OTS secret key $\mathsf{sk}_q = (\mathsf{otstype}, I, q, x_q)$ for $0 \leq q < 2^h$. Then, for each $q \in \{0, \cdots, 2^h - 1\}$,

we can derive its corresponding public key pk_q with Algorithm 1, from which we can derive $\mathsf{pk}_q.K.$

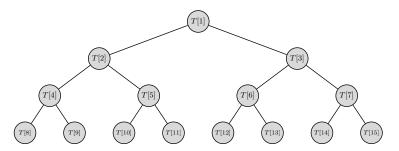


Fig. 1: An LMS tree with height 3

Let $K_q = \mathsf{pk}_q.K$. With these 2^h K_i 's, we can construct a height-h perfect binary tree with $2^{h+1}-1$ nodes labeled by $T[1], T[2], \dots, T[2^{h+1}-1]$. Figure 1 depicts a LMS tree with height 3. The values of T[j]'s are computed according to the following formula:

$$T[r] = \begin{cases} H(I||\text{u32str}(r)||\text{0x8282}||K_{r-2^h}), & r \ge 2^h \\ H(I||\text{u32str}(r)||\text{0x8383}||T[2r]||T[2r+1]), & 0 \le r < 2^h \end{cases} . \tag{2}$$

The LMS public key is (lmstype, otstype, I, T[1]) $\in \mathbb{B}^4 \times \mathbb{B}^4 \times \mathbb{B}^{16} \times \mathbb{B}^m$, where T[1] is the root of the associated LMS tree.

4.3 LMS Signature Generation

Given a message $M \in \mathbb{F}_2^*$ and an LMS secret key (lmstype, otstype, I, q, \mathbf{x}), the signature of M is

$$(u32str(q), \sigma_q(M), lmstype, (path[0], path[1], \cdots, path[h-1])),$$

where

 $sigma_q(M) = \texttt{LMOTS_GenSig}(M, (\texttt{lmstype}, \texttt{otstype}, I, q, \mathbf{x})), \text{ and }$

$$(path[0], \cdots, path[h-1])$$

is the authentication path of $T[2^h + q]$. For example, if h = 3 and q = 1, then (path[0], path[1], path[2]) = (T[8], T[5], T[3]) as shown in Figure 2.

4.4 LMS Signature Verification

Let $(u32str(q), \sigma_q(M), lms_type, (path[0], path[1], \cdots, path[h-1]))$ be the LMS signature of a message M. Then, we can compute the *hypothetical* value of the q-th leaf node $T'[2^h + q]$ from $\sigma_q(M)$. Then, with the information provided in

$$(path[0], path[1], \cdots, path[h-1]),$$

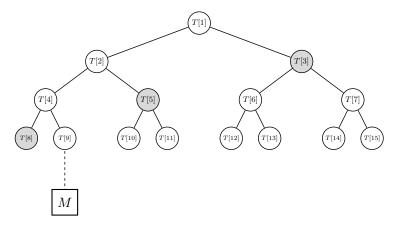


Fig. 2: An LMS tree with height 3

we can compute the *hypothetical* value T'[1] of the root. The signature is valid if and only if T[1] = T'[1]. After generating the signature, the signing process increments the q value in the private key by 1. This is why we say that LMS is a stateful signature scheme.

5 The Hierarchical Signature Scheme HSS

Like LMS, The HSS scheme is another method for organizing a large set of LM-OTS instances. The time complexity for generating an LMS key pair can be very high if the height of the corresponding LMS tree is large, since all of the tree nodes have to be computed to obtain the root.

The HSS signature scheme can be employed if we want to reduce the time taken by the key generation process. In HSS, LM-OTS instances are associated with the leaves of many LMS trees placed at different levels. The LMS trees are "connected" in the sense that the roots of the LMS trees are signed by the LM-OTS instances associated with the leaves of the LMS trees in the upper level. The leaves of the lowest level LMS trees are used to sign the messages. We call this structure an HSS tree or HSS instance. A 3-level HSS tree signing a message M is illustrated in Figure 3, where only the involved LMS trees are displayed.

In HSS, we have L layers of LMS instances, including layer $0, \dots,$ layer L-1. The LMS instances in the same layer have the same height. Let h_i be the height of the LMS trees in layer i. In the 0-th layer, there is only 1 LMS tree. For $1 \leq i < L$, there are $2^{\sum_{j=0}^{i-1}h_j}$ LMS trees in the i-th layer. Let $H = \sum_{j=0}^{L-1}h_j$, then there are 2^H leaves in the (L-1)-th layer, which correspond to 2^H LM-OTS keys. Such an HSS instance can sign at most 2^H times, and we call 2^h is the capacity. Note that a 1-level HSS instances is essentially an LMS instance.

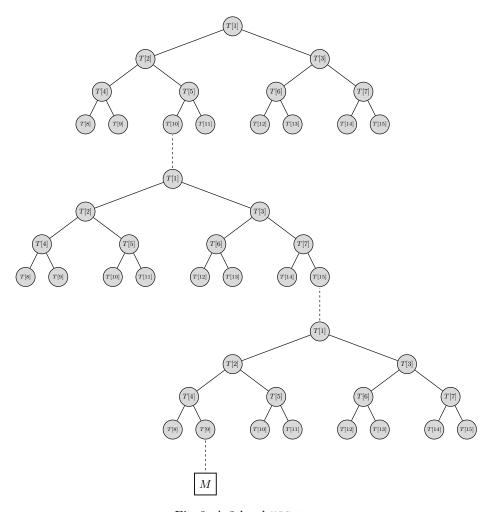


Fig. 3: A 3-level ${\tt HSS}$ tree

5.1 HSS Key Generation

First, using the method described in Section 4, we generate one LMS key pair. We store the private key into prv[0] and store the public key into pub[0].

For each $i \in \{1, 2, \cdots, L-1\}$, we independently generate an LMS key pair. We store the private key into prv[i] and store the public key into pub[i]. Also, we sign pub[i] with prv[i-1], and store the signature into sig[i-1]. Now, we have 3 arrays.

$$\begin{cases} \mathtt{prv} = (\mathtt{prv}[0], \mathtt{prv}[1], \cdots, \mathtt{prv}[L-2], \mathtt{prv}[L-1]) \\ \mathtt{pub} = (\mathtt{pub}[0], \mathtt{pub}[1], \cdots, \mathtt{pub}[L-2], \mathtt{pub}[L-1]) \\ \mathtt{sig} = (\mathtt{sig}[0], \mathtt{sig}[1], \cdots, \mathtt{sig}[L-2]) \end{cases} \tag{3}$$

The HSS private key is (prv, pub, sig), and the HSS public key is $u32str(L) \parallel pub[0]$.

5.2 HSS Signature Generation

There are 3 cases for different values of L. When L = 0, the signature is $\mathtt{u32str}(0) \parallel \mathtt{sig}[0]$. When L > 0, the signature is

```
u32str(Nspk) \parallel signed_pub_key[0] \parallel \cdots \parallel signed_pub_key[Nspk-1] \parallel sig[Nspk],
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where Nspk = L - 1 (Number of Signed Public Keys) denotes the number of signed LMS public keys. The above signature can be obtained by Algorithm 5.

Algorithm 5: Compute the HSS signature of a message M

```
1 d \leftarrow L
2 while \operatorname{prv}[d-1].q = 2^{\operatorname{prv}[d-1].h} do
3 d \leftarrow d-1
4 if d=0 then
5 \operatorname{return} \ \operatorname{FAILURE}
6 while d < L do
7 Randomly generate \operatorname{pub}[d] and \operatorname{prv}[d]
8 \operatorname{sig}[d-1] \leftarrow \operatorname{The} \ \operatorname{LMS} \ \operatorname{signature} \ \operatorname{of} \ \operatorname{pub}[d] \ \operatorname{signed} \ \operatorname{with} \ \operatorname{prv}[d-1]
9 d \leftarrow d+1
10 \operatorname{sig}[L-1] \leftarrow \operatorname{The} \ \operatorname{LMS} \ \operatorname{signature} \ \operatorname{of} \ M \ \operatorname{signed} \ \operatorname{with} \ \operatorname{prv}[L-1]
11 for 0 \le i < L-1 do
12 \operatorname{signed} \ \operatorname{pub} \ \operatorname{key}[i] \leftarrow \operatorname{sig}[i] \ \operatorname{pub}[i+1]
13 \operatorname{return} \ \operatorname{u32str}(L-1) \ \| \ \operatorname{signed} \ \operatorname{pub} \ \operatorname{key}[0] \ \| \ \cdots \ \| \ \operatorname{signed} \ \operatorname{pub} \ \operatorname{key}[L-2] \ \| \ \operatorname{sig}[L-1]
```

5.3 Signature Verification

The signature is valid if and only if all of

```
signed_pub_key[0], \cdots, signed_pub_key[L-2]
```

and sig[L-1] are valid.

6 Preliminary Implementations and Performance Test

We instantiate the hash-based signature schemes described in previous sections with SM3, and we name them as LMS-SM3 and HSS-SM3. We implement LMS-SM3 and HSS-SM3 based on the code provided at https://github.com/cisco/hash-sigs by substituting the underlying hash function with an implementation of SM3. The

performance of the implementation is provided in Table 8, which are obtained on a server machine with 32 cores running Linux ubuntu 18.04 on 2.9GHz AMD EPYC-Rome Processor.

In Table 8, the "Height" column records the heights of the LMS trees in LMS-SM3 or HSS-SM3, where a single number h means a LMS-SM3 instance with height h, and h_0/h_1 means a two level HSS-SM3 instance with height h_0 in the 0-th level and height h_1 in the 1st level.

7 Conclusion

In this work, we instantiate the hash-based signature schemes LMS and HSS described in RFC 8554 with SM3 and conduct some preliminary performance test. In the future, we will provide implementations of LMS-SM3, HSS-SM3, and XMSS-SM3 on various platforms and deploy them in real application scenarios to test the applicability of hash-based signature schemes.

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 \boldsymbol{w} ∞ 5 10 15 20 15/10 15/15 20/10 20/15 15/10 15/15 20/10 20/15Height 5 10 15 20 $\begin{array}{c} \texttt{KeyGenTime} \\ (s) \end{array}$ 0.033 0.697 21.35 928.21 23.95 25.62 911.42 960.46 0.011 0.098 2.91 100.02 2.99 3.18 107.35 118.06 PubKeySize 60 60 60 60 60 60 60 60 PrvKeySize 64 64 64 64 64SignTime (s) $0.0056 \\ 0.0079$ 0.019 0.019 0.01 0.01 0.013 0.011 0.024 0.042 0.01 0.09 0.056 0.068 0.057 SigSize (Byte) 2,352 2,512 2,672 2,832 2,832 5,236 5,396 5,396 5,536 1,296 1,456 1,616 1,776 3,124 3,284 3,284 3,444 $\begin{array}{c} \texttt{VerifyTime} \\ (s) \end{array}$ 0.0015 0.0014 0.0018 0.002 0.0034 0.0038 0.0038 0.0033 0.0036 0.0046 0.005 0.01 0.01 0.01 0.001 Capacity 2^{5} 2^{10} 2^{15} 2^{20} 2^{25} 2^{30} 2^{35} 2^{5} 2^{10} 2^{15} 2^{20} 2^{25} 2^{20} 2^{30} 2^{30} 2^{35}

Table 8: Preliminary performance test of HSS-SM3

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