# How To Find Many Collisions of 3-Pass HAVAL 

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#### Abstract

The hash function HAVAL is an Australian extension of well known Merkle-Damgård hash functions such as MD4 and MD5. It has three variants, 3-, 4- and 5-pass HAVAL. On 3-pass HAVAL, the best known attack finds a collision pair with $2^{7}$ computations of the compression function. To find $k$ collision pairs, it requires $2^{7} k$ computations. In this paper, we present a better collision attack on 3-pass HAVAL, which can find $k$ collision pairs with only $2 k+33$ computations. Further, our message differential is different from the previous ones. (It is important to find collisions for different message differentials.)


Key words: hash function, HAVAL, collision, differential attack

## 1 Introduction

The hash function HAVAL was proposed by Zheng, Pieprzyk, and Seberry at Auscrypt '92 [8]. It is an Australian extension of well known Merkle-Damgård hash functions such as MD4 and MD5. ${ }^{3}$ HAVAL has three variants, 3-, 4- and 5-pass HAVAL, which means that the compression function has 96,128 , and 160 rounds, respectively. The compression function $H$ of HAVAL takes a 256 -bit initial value and a 1024 -bit message $M=\left(m_{0}, \ldots, m_{31}\right)$ as input, and produces 256 -bit hash value as output, where each $m_{i}$ is a 32 -bit word.

On 3-pass HAVAL, Rompay, et al. [2] presented a collision attack that requires $2^{29}$ computations of the compression function. Their attack can find a one-block (1024-bit) collision pair $M=\left(m_{0}, \ldots, m_{31}\right)$ and $M^{\prime}=\left(m_{0}^{\prime}, \ldots, m_{31}^{\prime}\right)$ with the differential

$$
\Delta m_{28}=2^{0}=1 \text { and } \Delta m_{i}=0 \text { for the other } i
$$

X.Y.Wang et al. [4] showed a much better collision attack with $2^{7}$ computations of the compression function. Their attack can find a one-block collision pair $M=\left(m_{0}, \ldots, m_{31}\right)$ and $M^{\prime}=\left(m_{0}^{\prime}, \ldots, m_{31}^{\prime}\right)$ with the differential

$$
\Delta m_{0}=2^{10}, \Delta m_{11}=2^{31}, \Delta m_{18}=2^{3}, \text { and } \Delta m_{i}=0 \text { for the other } i
$$

[^0]To find $k$ collision pairs of 3-pass HAVAL, the best known attack [4] requires $2^{7} k$ computations.

In this paper, we present a better collision attack on 3-pass HAVAL which can find $k$ collision pairs with only $2 k+33$ computations. Further, our message differential is different from the previous ones. ${ }^{4}$ (It is important to find collisions for different message differentials.)

The previous attacks $[2,4]$ are one-block collision attacks (i.e. a collision pair is a pair of 1024-bit message block). On the other hand, our attack is a two-block collision attack which can find a two-block (2048-bit) collision pair $M_{0} \| M_{1}=$ $\left(m_{0,0}, \ldots, m_{0,31}, m_{1,0}, \ldots, m_{1,31}\right)$ and $M_{0}^{\prime} \| M_{1}^{\prime}=\left(m_{0,0}^{\prime}, \ldots, m_{0,31}^{\prime}, m_{1,0}^{\prime}, \ldots\right.$, $m_{1,31}^{\prime}$ ) with the differential

$$
\Delta m_{j, i}=m_{j, i}^{\prime}-m_{j, i} \bmod 2^{32}= \begin{cases}2^{31} & \text { if } i=5 \\ 0 & \text { otherwise }\end{cases}
$$

In our attack, we first find a near-collision pair $\left(M_{0}, M_{0}^{\prime}\right)$ such that $H\left(M_{0}\right)$ and $H\left(M_{0}^{\prime}\right)$ are almost the same. We then find many full collision pairs $\left(M_{0} \| M_{1}\right.$, $\left.M_{0}^{\prime} \| M_{1}^{\prime}\right)$ by using the freedom of ( $M_{1}, M_{1}^{\prime}$ ). Theoretically, our near-collision pair can be found by about 33 computations of the compression function. Once a near collision pair is found, a full collision pair can be found with probability $1 / 2$. Hence we can find $k$ collision pairs with $2 k+33$ computations. (See Table 1.)

|  | Rompay, et al. [2] | X.Y.Wang et al. [7] | Proposed |
| :---: | :---: | :---: | :---: |
| $\Delta m_{i}$ | $\Delta m_{28}=2^{0}=1$ | $\Delta m_{0}=2^{10}$ <br> $\Delta m_{11}=2^{31}$ <br> $\Delta m_{18}=2^{3}$ | $\Delta m_{0,5}=2^{31}$ <br> $\Delta m_{1,5}=2^{31}$ <br> complexity for first collision |
|  | $2^{29}$ | $2^{29} k$ | $2+33$ |
|  | 1024 bits | 1024 bits | 2048 bits |

Table 1. Collision attacks on 3-pass HAVAL

In our personal computer simulation:

1. We found 15147 near-collision pairs by 500000 trials, which agrees with our theoretical estimate because $500000 / 15147=33.0098 \cdots$.
2. From a single near-collision pair, we found 249630 full collision pairs by 500000 trials, which also agrees with our theoretical complexity because $500000 / 249630 \approx 2$.
[^1]It took about one minute for the first 500000 trials. It also took about one minute for the next 500000 trials.

## (Related wroks:)

- Modular differential attack was presented in 1997 by X.Y.Wang [3] and formalized in Eurocrypt ' 05 [5,6]. They showed that it is very powerful to break MD4, MD5, SHA-0, SHA-1 and HAVAL. Our attack is also based on the modular differential approach.
- On 4-pass HAVAL, H.Yu et al. [7] showed two two-block collision attacks that require $2^{43}$ and $2^{36}$ computations of 4 -pass HAVAL, respectively. On 5-pass HAVAL, the H.Yu et al. [7] showed a one-block collision attack with $2^{123}$ computations of the compression function.

This paper is organized as follows. In Section 2, we provide a simple description of 3-pass HAVAL. In Section 3, we give an outline of our attack. In Section 4 , we present the algorithm of our attack, and calculate the complexity. In Section 5, we report on our computational experiment and a collision example. In Section 6, we conclude this paper. In this paper, almost Tables and Figures are in the Appendix.

## 2 3-Pass HAVAL

HAVAL consists of three phases: (1) message padding phase, (2) main hashing phase and (3) optional compression phase.

### 2.1 Message Padding Phase

HAVAL pads an input message by appending some bit string so that its bitlength becomes a multiple of 1024.

### 2.2 Main Hashing Phase

HAVAL is a Merkle-Damgård hash function based on a compression function $H$ as follows. Let $M_{0}\left\|M_{1}\right\| \cdots \| M_{t}$ be the padded message, where $\left|M_{i}\right|=1024$. Then for $i=0, \cdots, t$, compute

$$
I V_{i+1}=H\left(I V_{i}, M_{i}\right)
$$

where $\left|I V_{i}\right|=256$ and $I V_{0}=(a, b, c, d, e, f, g, h)$ is the initial value such that

$$
\begin{aligned}
& a=0 x 243 f 6 a 88, b=0 x 85 a 308 d 3, c=0 x 13198 a 2 e, d=0 x 03707344, \\
& e=0 x a 4093822, f=0 x 299 f 31 d 0, g=0 x 082 e f a 98, h=0 x e c 4 e 6 c 89 .
\end{aligned}
$$

The hashed value is given by $I V_{t+1}$.
$H$ is described as follows. First define three functions as follows.

$$
\begin{aligned}
F_{1}\left(x_{0}, x_{1}, x_{2}, x_{3}, x_{4}, x_{5}, x_{6}\right)=\left(x_{2} \bullet x_{3}\right) & \oplus\left(x_{2} \bullet x_{4}\right) \oplus x_{4} \oplus\left(x_{0} \bullet x_{6}\right) \oplus\left(x_{1} \bullet x_{5}\right), \\
F_{2}\left(x_{0}, x_{1}, x_{2}, x_{3}, x_{4}, x_{5}, x_{6}\right)=\left(x_{0} \bullet x_{2}\right) & \oplus\left(x_{1} \bullet x_{2}\right) \oplus\left(x_{1} \bullet x_{3}\right) \oplus\left(x_{0} \bullet x_{3} \bullet x_{5}\right) \\
& \oplus\left(x_{1} \bullet x_{2} \bullet x_{5}\right) \oplus\left(x_{3} \bullet x_{5}\right) \oplus\left(x_{4} \bullet x_{5}\right) \\
& \oplus x_{6} \oplus\left(x_{5} \bullet x_{6}\right), \\
F_{3}\left(x_{0}, x_{1}, x_{2}, x_{3}, x_{4}, x_{5}, x_{6}\right)=x_{0} \quad & \oplus\left(x_{0} \bullet x_{3}\right) \oplus\left(x_{1} \bullet x_{4}\right) \oplus\left(x_{2} \bullet x_{5}\right) \\
& \oplus\left(x_{3} \bullet x_{4} \bullet x_{5}\right) \oplus\left(x_{3} \bullet x_{6}\right),
\end{aligned}
$$

where $x_{i}$ is a 32-bit word, $x_{i} \bullet x_{j}$ is the bit-wise multiplication of $x_{i}$ and $x_{j}$, and $x_{i} \oplus x_{j}$ is the bit-wise modulo 2 addition.
$H$ next runs the following algorithm $\tilde{H}$ on input

$$
\begin{aligned}
I V & =\left(a_{0}, b_{0}, c_{0}, d_{0}, e_{0}, f_{0}, g_{0}, h_{0}\right) \\
M & =\left(m_{0}, m_{1}, \ldots, m_{31}\right)
\end{aligned}
$$

where each of $a_{0}, \ldots, h_{0}$ and $m_{i}$ is a 32 -bit word.
$\operatorname{For}(i=0$ to 95$)\{$

$$
\begin{align*}
j & :=\lfloor i / 32\rfloor+1 ; \\
p_{i} & :=F_{j}\left(a_{i}, b_{i}, c_{i}, d_{i}, e_{i}, f_{i}, g_{i}\right) ; \\
a_{i+1} & :=\left(p_{i} \gg 7\right)+\left(h_{i} \gg 11\right)+m_{\operatorname{ord}(i)}+k_{i} \bmod 2^{32} ;  \tag{1}\\
b_{i+1} & :=a_{i}, c_{i+1}:=b_{i}, d_{i+1}:=c_{i}, e_{i+1}:=d_{i}, \\
f_{i+1} & :=e_{i}, g_{i+1}:=f_{i}, h_{i+1}:=g_{i}
\end{align*}
$$

## \}

where $x \gg s$ denotes the $s$-bit right rotation of $x,+$ denotes the modulo $2^{32}$ addition, and the word processing orders $\operatorname{ord}(i)$ and the constant values $k_{i}$ are given in Table 3 . Note that $\tilde{H}$ consists of 96 rounds, 0 -round through 95 -round.

Finally, $H$ outputs the following 256 -bit value

$$
\begin{aligned}
& I V+\tilde{H}(I V, M) \\
& =\left(a_{0}+a_{96}, b_{0}+b_{96}, c_{0}+c_{96}, d_{0}+d_{96}, e_{0}+e_{96}, f_{0}+f_{96}, g_{0}+g_{96}, h_{0}+h_{96}\right) .
\end{aligned}
$$

Figure 1 is an outline sketch of $H$. In the Appendix, we provide more detailed sketches for each round. (See Figure 2, 3, and 4.)

### 2.3 Optional Compression Phase

HAVAL supports hash-sizes of 128, 160, 192, 224 and 256 bits. The main algorithm computes 256 -bit hash-values, and the other sizes are obtained by postprocessing the 256 -bit hash-value.


Fig. 1. The compression function $H$ of 3-pass HAVAL.

## 3 Outline of our Attack

### 3.1 Notation

For $H(I V, M), a_{i}, b_{i}, \cdots$ denote the local values which appear in $i$-round. Similarly, for $H\left(I V, M^{\prime}\right), a_{i}^{\prime}, b_{i}^{\prime}, \cdots$ denote the local values which appear in $i$-round. We denote by $a a_{0}, b b_{0}, c c_{0}, d d_{0}, e e_{0}, f f_{0}, g g_{0}, h h_{0}$ the 8 words of $I V_{1}$. Define $\Delta a_{i}=a_{i}^{\prime}-a_{i} \bmod 2^{32}$, and so on.

We denote by $x_{i, j}$ the $j$-th bit of 32 -bit word $x_{i}$.
$-x_{i}^{\prime}=x_{i}[j]$ means that $x_{i}^{\prime}$ is obtained by changing the $j$ th bit of $x_{i}$ from 0 to 1. That is, $x_{i}^{\prime}=x_{i}$ except for that $x_{i, j}=0$ and $x_{i, j}^{\prime}=1$.
$-x_{i}^{\prime}=x_{i}[-j]$ means that $x_{i}^{\prime}$ is obtained by changing the $j$ th bit of $x_{i}$ from 1 to 0 . That is, $x_{i}^{\prime}=x_{i}$ except for that $x_{i, j}=1$ and $x_{i, j}^{\prime}=0$.
$-x_{i}^{\prime}=x_{i}[ \pm j]$ means that $x_{i, j} \neq x_{i, j}^{\prime}$.

- For example, $a_{14}[-21,22]$ is the value obtained by modifying the 21-th and 22 -th bit of $a_{14}$ from 1 to 0 and 0 to 1 , respectively.


### 3.2 Attack

We show an efficient method to find a two-block (2048-bit) collision pair

$$
\begin{aligned}
& M_{0} \| M_{1}=\left(m_{0,0}, \ldots, m_{0,31}, m_{1,0}, \ldots, m_{1,31}\right) \\
& M_{0}^{\prime} \| M_{1}^{\prime}=\left(m_{0,0}^{\prime}, \ldots, m_{0,31}^{\prime}, m_{1,0}^{\prime}, \ldots, m_{1,31}^{\prime}\right) .
\end{aligned}
$$

The proposed method first finds a near collision pair ( $M_{0}, M_{0}^{\prime}$ ) such that

$$
\Delta I V_{1}=I V_{1}^{\prime}-I V_{1}=\left(0,2^{31}, 0,0,0,0,0,0\right)
$$

We next find a pair $\left(M_{1}, M_{1}^{\prime}\right)$ such that

$$
\begin{align*}
\Delta A & =\tilde{H}\left(I V_{1}^{\prime}, M_{1}^{\prime}\right)-\tilde{H}\left(I V_{1}, M_{1}\right) \\
& =\left(0,2^{31}, 0,0,0,0,0,0\right) \text { or }\left(0,-2^{31}, 0,0,0,0,0,0\right) \tag{2}
\end{align*}
$$

Then it holds that

$$
\begin{equation*}
H\left(I V_{1}^{\prime}, M_{1}^{\prime}\right)=I V_{1}^{\prime}+\tilde{H}\left(I V_{1}^{\prime}, M_{1}^{\prime}\right)=I V_{1}+\tilde{H}\left(I V_{1}, M_{1}\right)=H\left(I V_{1}, M_{1}\right) \tag{3}
\end{equation*}
$$

That is,

$$
\Delta I V_{0}=0 \xrightarrow{\left(M_{0}, M_{0}^{\prime}\right)} \Delta I V_{1} \xrightarrow{\left(M_{1}, M_{1}^{\prime}\right)} \Delta A \rightarrow \Delta H=0
$$

Therefore, $\left(M_{0}\left\|M_{1}, M_{0}^{\prime}\right\| M_{1}^{\prime}\right)$ is a collision pair. ${ }^{5}$
We use a message differential such that

$$
\Delta m_{j, i}=m_{j, i}^{\prime}-m_{j, i} \bmod 2^{32}= \begin{cases}2^{31} & \text { if } i=5 \\ 0 & \text { otherwise }\end{cases}
$$

for $j=0$ and $1 .{ }^{6}$ That is,

$$
\begin{aligned}
& \Delta M_{0}=\left(0,0,0,0,0,2^{31}, 0, \cdots, 0\right) \\
& \Delta M_{1}=\left(0,0,0,0,0,2^{31}, 0, \cdots, 0\right)
\end{aligned}
$$

Note that $m_{5}$ is the input to the 5 -, 32 -, and 94 -round in each block because

$$
5=\operatorname{ord}(5)=\operatorname{ord}(32)=\operatorname{ord}(94)
$$

from Table 3. Now we will find the first block pair $\left(M_{0}, M_{0}^{\prime}\right)$ that causes a local collision at the 32 -round. Then $\left(M_{0}, M_{0}^{\prime}\right)$ is automatically a near collision pair just after 94 -round with difference $\left(0, \pm 2^{31}, 0,0,0,0,0,0\right)$. This can be seen from the following table.

| round | 0 | $\cdots$ | 5 | $\cdots$ | 32 | $\cdots$ | 94 | 95 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\Delta m_{i}$ | $\Delta m_{0}=0$ | $\cdots$ | $\Delta m_{5}=2^{31}$ | $\cdots$ | $\Delta m_{5}=2^{31}$ | $\cdots$ | $\Delta m_{5}=2^{31}$ | $\cdots$ |
| $\tilde{H}(I V, M)$ |  |  |  |  | collision |  | near collision | near collision |

Similarly we will find the second block pair ( $M_{1}, M_{1}^{\prime}$ ) which satisfy eq.(2), where $I V_{1}=H\left(I V_{0}, M_{0}\right)$ and $I V_{1}^{\prime}=H\left(I V_{0}, M_{0}^{\prime}\right)$. Then $M_{0} \| M_{0}^{\prime}$ and $M_{1} \| M_{1}^{\prime}$ are a full collision pair from eq.(3).

We present the (so called) differential path in Table 4 and Table 5. ${ }^{7}$ In these Table, for example,

| round $i$ | $m_{i}^{\prime}$ | $\Delta a_{i+1}$ | Outputs $a_{i}^{\prime}, b_{i}^{\prime}, c_{i}^{\prime}, d_{i}^{\prime}, e_{i}^{\prime}, f_{i}^{\prime}, g_{i}^{\prime}, h_{i}^{\prime}$ |
| :---: | :---: | :---: | :--- |
| 6 | $m_{6}$ | 0 | $a_{7}, a_{6}[32], a_{5}, a_{4}, a_{3}, a_{2}, a_{1}, a_{0}$ |

means that we want the outputs $\left(a_{7}^{\prime}, b_{7}^{\prime}, c_{7}^{\prime}, d_{7}^{\prime}, e_{7}^{\prime}, f_{7}^{\prime}, g_{7}^{\prime}, h_{7}^{\prime}\right)$ in the 6 -round of $H\left(I V^{\prime}, M^{\prime}\right)$ to be $\left(a_{7}, b_{7}[32], c_{7}, d_{7}, e_{7}, f_{7}, g_{7}, h_{7}\right)$. Note that $\left(a_{7}, b_{7}, c_{7}, d_{7}, e_{7}\right.$, $\left.f_{7}, g_{7}, h_{7}\right)=\left(a_{7}, a_{6}, a_{5}, a_{4}, a_{3}, a_{2}, a_{1}, a_{0}\right)$. We can find a full collision if all the conditions of these tables are satisfied.

[^2]
### 3.3 Sufficient Conditions

In Table 6, 7, and 8, we present sufficient conditions for the differential path to hold. If Table 6,7 , and 8 are satisfied, then Table 4 and 5 are satisfied. As an example, we prove that the conditions for 5 - and 6 -round given in Table 6 guarantee that the conditions for 0 - to 6 -round shown in Table 4. The other conditions are derived similarly.

Since $\Delta m_{0}=\cdots=\Delta m_{4}=0$, the differential path of 0 - to 4 -round hold. In 5 -round of $H\left(I V_{0}^{\prime}, M_{0}^{\prime}\right)$, if the sufficient condition of 5 -round in Table 6, that is, $a_{6,32}=0$, then $a_{6,32}^{\prime}=1$ and $a_{6, i}^{\prime}=a_{6, i}$ for $i \neq 32$ (i.e. $a_{6}^{\prime}=a_{6}[32]$ ), because

$$
\begin{aligned}
a_{6} & =\left(p_{5} \gg 7\right)+\left(h_{5} \gg 11\right)+m_{\text {ord }(5)}+k_{5} \\
a_{6}^{\prime} & =\left(p_{5}^{\prime} \gg 7\right)+\left(h_{5}^{\prime} \gg 11\right)+m_{\text {ord }(5)}^{\prime}+k_{5} \\
& =\left(p_{5} \gg 7\right)+\left(h_{5} \gg 11\right)+\left(m_{\text {ord }(5)}+2^{31}\right)+k_{5} \\
& =\left(p_{5} \gg 7\right)+\left(h_{5} \gg 11\right)+m_{\text {ord }(5)}+k_{5}+2^{31} \\
& =a_{6}+2^{31} .
\end{aligned}
$$

In 6-round of $H\left(I V_{0}^{\prime}, M_{0}^{\prime}\right)$, if the sufficient condition of 5 -round in Table 6, that is, $a_{0,32}=0$ then, since

$$
\begin{aligned}
p_{6} & =F_{1}\left(a_{6}, b_{6}, c_{6}, d_{6}, e_{6}, f_{6}, g_{6}\right) \\
& =F_{1}\left(a_{6}, a_{5}, a_{4}, a_{3}, a_{2}, a_{1}, a_{0}\right) \\
& =\left(a_{4} \bullet a_{3}\right) \oplus\left(a_{4} \bullet a_{2}\right) \oplus a_{2} \oplus\left(a_{6} \bullet a_{0}\right) \oplus\left(a_{5} \bullet a_{1}\right),
\end{aligned}
$$

we have

$$
\begin{aligned}
p_{6,32} & =\left(a_{4,32} \bullet a_{3,32}\right) \oplus\left(a_{4,32} \bullet a_{2,32}\right) \oplus a_{2,32} \oplus\left(a_{6,32} \bullet a_{0,32}\right) \oplus\left(a_{5,32} \bullet a_{1,32}\right), \\
& =\left(a_{4,32} \bullet a_{3,32}\right) \oplus\left(a_{4,32} \bullet a_{2,32}\right) \oplus a_{2,32} \oplus(0 \bullet 0) \oplus\left(a_{5,32} \bullet a_{1,32}\right), \\
& =\left(a_{4,32} \bullet a_{3,32}\right) \oplus\left(a_{4,32} \bullet a_{2,32}\right) \oplus a_{2,32} \oplus 0 \oplus\left(a_{5,32} \bullet a_{1,32}\right), \\
p_{6,32}^{\prime} & =\left(a_{4,32}^{\prime} \bullet a_{3,32}^{\prime}\right) \oplus\left(a_{4,32}^{\prime} \bullet a_{2,32}^{\prime}\right) \oplus a_{2,32}^{\prime} \oplus\left(a_{6,32}^{\prime} \bullet a_{0,32}^{\prime}\right) \oplus\left(a_{5,32}^{\prime} \bullet a_{1,32}^{\prime}\right), \\
& =\left(a_{4,32}^{\prime} \bullet a_{3,32}^{\prime}\right) \oplus\left(a_{4,32}^{\prime} \bullet a_{2,32}^{\prime}\right) \oplus a_{2,32}^{\prime} \oplus(1 \bullet 0) \oplus\left(a_{5,32}^{\prime} \bullet a_{1,32}^{\prime}\right), \\
& =\left(a_{4,32}^{\prime} \bullet a_{3,32}^{\prime}\right) \oplus\left(a_{4,32}^{\prime} \bullet a_{2,32}^{\prime}\right) \oplus a_{2,32}^{\prime} \oplus 0 \oplus\left(a_{5,32}^{\prime} \bullet a_{1,32}^{\prime}\right),
\end{aligned}
$$

Hence, $p_{6}^{\prime}=p_{6}$. Therefore $a_{7}^{\prime}=a_{7}$. The above equations for $p_{6,32}$ and $p_{6,32}^{\prime}$ are clear by Figure 2.

## 4 Details

In this section, we present the details of our algorithm, and calculate the complexity to find a collision pair.

### 4.1 Our Algorithm

We observe that from $a_{1}, \cdots, a_{32}, M_{0}=\left(m_{0}, \ldots, m_{31}\right)$ is uniquley determined from eq.(1), and $a_{33}, \cdots, a_{96}$ are also uniquely determined. Now in Table 6, all the rows except the last three rows specify the conditions on $a_{1}, \cdots, a_{32}$. Hence:

1. We choose $a_{1}, \cdots, a_{32}$ which satisfy these conditions randomly.
2. We compute $M_{0}=\left(m_{0}, \ldots, m_{31}\right)$ from eq.(1). ${ }^{8}$
3. If the last three rows are also satisfied, then we have done.

Next for given $M_{0}$, we apply the same strategy to find $M_{1}$.

1. We choose $a_{1}, \cdots, a_{32}$ which satisfy the conditions of Table 7 and Table 8 randomly.
2. We compute $M_{1}$ from eq.(1).
3. If the last row of Table 8 is also satisfied, then we have done.

## Finding $M_{0}$ :

1. Randomly select $a_{1}, \ldots, a_{32}$
that satisfy the sufficient conditions for $0-31$ rounds.
2. For $i=0$ to 31,
$b_{i+1}:=a_{i}, c_{i+1}:=b_{i}, d_{i+1}:=c_{i}, e_{i+1}:=d_{i}$,
$f_{i+1}:=e_{i}, g_{i+1}:=f_{i}, h_{i+1}:=g_{i}$.
3. Calculate $p_{0}, \ldots, p_{31}$ of the algorithm of $H$ in Section 2
and $m_{0}, \ldots, m_{31}$ as follows, $p_{i}:=F_{1}\left(a_{i}, b_{i}, c_{i}, d_{i}, e_{i}, f_{i}, g_{i}\right)$, $m_{i}:=a_{i+1}-\left(p_{i} \gg 7\right)-\left(h_{i} \gg 11\right)-k_{i} \bmod 2^{32}$.
4. Execute 32 - to 95 -round of the compression function.
5. If $a_{95,32}=1, a_{92,32}=1, b b_{0,32}=0, f f_{0,32}=0$,
$c c_{0,32}=d d_{0,32}$, and $a a_{0,32}=0$,
then fix $M_{0}=\left(m_{0}, \ldots, m_{31}\right)$.

## Finding $M_{1}$ :

6. Randomly select $a_{1}, \ldots, a_{32}$
that satisfy the sufficient conditions for $0-31$ rounds.
7. For $i=0$ to 31 ,
$b_{i+1}:=a_{i}, c_{i+1}:=b_{i}, d_{i+1}:=c_{i}, e_{i+1}:=d_{i}$, $f_{i+1}:=e_{i}, g_{i+1}:=f_{i}, h_{i+1}:=g_{i}$.
8. Calculate $p_{0}, \ldots, p_{31}$ of the algorithm of $H$ in Section 2 and $m_{0}, \ldots, m_{31}$ as follows,
$p_{i}:=F_{1}\left(a_{i}, b_{i}, c_{i}, d_{i}, e_{i}, f_{i}, g_{i}\right)$,
$m_{i}:=a_{i+1}-\left(p_{i} \gg 7\right)-\left(h_{i} \gg 11\right)-k_{i} \bmod 2^{32}$.
9. Execute 32 - to 95 -round of the compression function.
10. If $a_{92,32}=1$, then output $\left(M_{0} \| M_{1}\right)$ and $\left(M_{0}^{\prime} \| M_{1}^{\prime}\right)$ as a collision pair.

### 4.2 Success Probability

Assume that

$$
\begin{equation*}
\operatorname{Pr}\left[x_{i, j}=0\right]=\operatorname{Pr}\left[x_{i, j}=1\right]=1 / 2 \tag{4}
\end{equation*}
$$

[^3]for any word $x_{i}$. We can find $M_{0}$ if the last three condition are satisfied in Table 6 . Thereore, the success probability $P$ of finding $M_{0}$ is given by
\[

$$
\begin{aligned}
P & =\operatorname{Pr}\left[a_{95,32}=1, a_{92,32}=1, a a_{0,32}=0, b b_{0,32}=0, c c_{0,32}=d d_{0,32}, f f_{0,32}=0,\right. \\
& =1 / 2^{5} \times \operatorname{Pr}\left[b b_{0,32}=0\right]
\end{aligned}
$$
\]

For $b b_{0}$, note that

$$
b b_{0}=b_{0}+b_{96}=b+a_{95}=(10000101 \cdots)+(1 ? ? ? ? ? ? ? \cdots) .
$$

Thus, if $a_{95,31}, a_{95,30}, a_{95,29}$, or $a_{95,28}$ is 0 , or $a_{95,31}=a_{95,30}=a_{95,29}=a_{95,28}=1$ and $a_{95,27}=a_{95,26}=0$, then $b b_{0,32}=0$. Hence

$$
\begin{aligned}
& \operatorname{Pr}\left[b b_{0,32}=0\right] \\
\geq & \operatorname{Pr}\left[a_{95,31}=0, a_{95,30}=0, a_{95,29}=0, \text { or } a_{95,28}=0\right] \\
& +\operatorname{Pr}\left[a_{95,31}=a_{95,30}=a_{95,29}=a_{95,28}=1 \text { and } a_{95,27}=a_{95,26}=0\right] \\
= & \left(1-\operatorname{Pr}\left[a_{95,31}=1, a_{95,30}=1, a_{95,29}=1, \text { and } a_{95,28}=1\right]\right)+1 / 2^{6} \\
= & \left(1-1 / 2^{4}\right)+1 / 64=15 / 16+1 / 64=61 / 64 .
\end{aligned}
$$

Therefore

$$
P \geq 1 / 2^{5} \times 61 / 64=61 / 2^{11} \approx 1 / 33
$$

Next suppose that the above $M_{0}$ is given. Then we can find $M_{1}$ if the last row of Table 8 is satisfied. Thereore, the success probability of finding $M_{1}$ is given by

$$
\operatorname{Pr}\left[a_{92,32}=1\right]=1 / 2
$$

### 4.3 How to Find Many Collisions

We can find many collision pairs from fixed ( $M_{0}, M_{0}^{\prime}$ ) by running the algorithm "Finding $M_{1}$ " many times. In this method, the complexity of finding $k$ collision pairs is $2 k+33$.

## 5 Computational experiment

We implemented our attack by a personal computer. First we found 15,147 desired $M_{0}$ s by running the algorithm "Finding $M_{0} " 500,000$ times. In this experiment, the success probability $15,147 / 500,000 \approx 1 / 33$. It coincides with our theoretical probability shown in Section 3.

Next for fixed $M_{0}$, we found 249,630 desired $M_{1}$ s by running the algorithm "Finding $M_{1} " 500,000$ times. ${ }^{9}$ In this experiment, the success probability $249,630 / 500,000 \approx 1 / 2$. It coincides with our theoretical probability shown in Section 3.

In total, we found 249,630 full collision pairs by running the algorithms "Finding $M_{0}$ " 39 times and "Finding $M_{1} " 500,000$ times.

Consequently, our experiment supports our claim that we can find $k$ collision pairs with $2 k+33$ computations of the compression functions. We illustrate one of the 249630 collision pairs in Table 2.

[^4]| $M_{0}$ | c7f10962 08cf4e0c ddfd60a8 597cbd0d b050440c 205560d0 84569b2f 43b834dc $1270 d 097$ 2b027ff7 32247646 8056892d 906feca6 a0a6b4ec fbc11aca d12586db f7e7bae1 ca89b85f 2d5a3e0f 8b4557da 8596d1bb 2bf5e1fd b5b7f669 9445ea09 343860ec 5c746759 bbce300c d0985871 5229b382 8dab9e3e f89f39d6 9179329b |
| :---: | :---: |
| 1 | cc4e7f72 c195d858 e5e2baf1 af7db590 84ddea8e 5990fd91 f6865ea5 9db928ce d3555dbd 6bf9b53a 694e5fff e96766dc 2d541b98 d394d721 6a84b2c2 0d2bd1a1 3afdac64 f0f67f58 60dd3e5d aec84176 575012f1 24878a2f 304720ed 25eed9ae 447f0e6e b03eaa86 9fa12c2a e98b9370 2e5cb01c a2e23d56 cdaf12f2 2efb842d |
| $M_{0}^{\prime}$ | c7f10962 08cf4e0c ddfd60a8 597cbd0d b050440c a05560d0 84569b2f 43b834dc <br> 1270 d097 2b027ff7 32247646 8056892d 906feca6 a0a6b4ec fbc11aca d12586db <br> f7e7bae1 ca89b85f 2d5a3e0f 8b4557da 8596d1bb 2bf5e1fd b5b7f669 9445ea09 <br> 343860ec 5c746759 bbce300c d0985871 5229b382 8dab9e3e f89f39d6 9179329b |
| $M_{1}$ | cc4e7f72 c195d858 e5e2baf1 af7db590 84ddea8e d990fd91 f6865ea5 9db928ce d3555dbd 6bf9b53a 694e5fff e96766dc 2d541b98 d394d721 6a84b2c2 0d2bd1a1 3afdac64 f0f67f58 60dd3e5d aec84176 575012f1 24878a2f 304720ed 25eed9ae 447f0e6e b03eaa86 9fa12c2a e98b9370 2e5cb01c a2e23d56 cdaf12f2 2efb842d |
| $H$ | c9f26b47 513d34a2 0ad20a17 3d207470 04848b80 fc90cc0a ef1cf172 d48c0d25 |

Table 2. Collision example.

## 6 Conclusion

On 3-pass HAVAL, the best known attack finds a collision pair with $2^{7}$ computations of the compression function. To find $k$ collision pairs, it requires $2^{7} k$ computations.

In this paper, we presented a better collision attack on 3-pass HAVAL using modular differential method. It can find $k$ collision pairs with only $2 k+33$ computations. Further, our message differential is different from the previous ones. (It is important to find collision pairs for different message differentials.)

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## Appendix : Tables and Figures

| i | ord (i) |
| :---: | :---: |
| 0 to 31 | 0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 <br> 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 |
| 32 to 63 | $\begin{array}{cccccccccccccccc} \hline 5 & 14 & 26 & 18 & 11 & 28 & 7 & 16 & 0 & 23 & 20 & 22 & 1 & 10 & 4 & 8 \\ 30 & 3 & 21 & 9 & 17 & 24 & 29 & 6 & 19 & 12 & 15 & 13 & 2 & 25 & 31 & 27 \end{array}$ |
| 64 to 95 | $\begin{array}{cccccccccccccccc} \hline 19 & 9 & 4 & 20 & 28 & 17 & 8 & 22 & 29 & 14 & 25 & 12 & 24 & 30 & 16 & 26 \\ 31 & 15 & 7 & 3 & 1 & 0 & 18 & 27 & 13 & 6 & 21 & 10 & 23 & 11 & 5 & 2 \end{array}$ |


| $\imath$ | $k_{i}$ |
| :---: | :---: |
| 0 to 31 | 00000000 |
| 32 to 63 | $452821 e 6$ 38d01377 be5466cf 34e90c6c c0ac29b7 c97c50dd 3f84d5b5 b5470917 9216d5d9 8979fb1b d1310ba6 98dfb5ac 2ffd72db d01adfb7 b8e1afed 6a267e96 ba7c9045 f12c7f99 24a19947 b3916cf7 0801f2e2 858efc16 636920d8 71574e69 a458fea3 f4933d7e 0d95748f 728eb658 718bcd58 82154aee 7b54a41d c25a59b5 |
| 64 to 95 | 9c30d539 2af26013 c5d1b023 $286085 f 0$ ca417918 b8db38ef 8e79dcb0 603a180e 6c9e0e8b b01e8a3e d71577c1 bd314b27 78af2fda 55605c60 e65525f3 aa55ab94 57489862 63e81440 55ca396a 2aab10b6 b4cc5c34 1141e8ce a15486af 7c72e993 b3ee1411 636fbc2a 2ba9c55d 741831f6 ce5c3e16 9b87931e afd6ba33 6c24cf5c |

Table 3. Word processing orders $\operatorname{ord}(i)$ and constant values $k_{i}$ (hexadecimal numbers).


Fig. 2. $i$-round $(0 \leq i \leq 31)$ in the compression function.


Fig. 3. $i$-round ( $32 \leq i \leq 63$ ) in the compression function.


Fig. 4. $i$-round ( $64 \leq i \leq 95$ ) in the compression function.

| round $i$ | $m_{i}^{\prime}$ | $\Delta a_{i+1}$ | Outputs $a_{i}^{\prime}, b_{i}^{\prime}, c_{i}^{\prime}, d_{i}^{\prime}, e_{i}^{\prime}, f_{i}^{\prime}, g_{i}^{\prime}, h_{i}^{\prime}$ |
| :---: | :---: | :---: | :---: |
| $I V_{0}^{\prime}$ |  |  | $a_{0}, b_{0}, c_{0}, d_{0}, e_{0}, f_{0}, g_{0}, h_{0}$ |
| 0 | $m_{0}$ | 0 | $a_{1}, a_{0}, b_{0}, c_{0}, d_{0}, e_{0}, f_{0}, g_{0}$ |
| 1 | $m_{1}$ | 0 | $a_{2}, a_{1}, a_{0}, b_{0}, c_{0}, d_{0}, e_{0}, f_{0}$ |
| 2 | $m_{2}$ | 0 | $a_{3}, a_{2}, a_{1}, a_{0}, b_{0}, c_{0}, d_{0}, e_{0}$ |
| 3 | $m_{3}$ | 0 | $a_{4}, a_{3}, a_{2}, a_{1}, a_{0}, b_{0}, c_{0}, d_{0}$ |
| 4 | $m_{4}$ | 0 | $a_{5}, a_{4}, a_{3}, a_{2}, a_{1}, a_{0}, b_{0}, c_{0}$ |
| 5 | $m_{5}^{\prime}$ | $2^{31}$ | $a_{6}[32], a_{5}, a_{4}, a_{3}, a_{2}, a_{1}, a_{0}, b_{0}$ |
| 6 | $m_{6}$ | 0 | $a_{7}, a_{6}[32], a_{5}, a_{4}, a_{3}, a_{2}, a_{1}, a_{0}$ |
| 7 | $m_{7}$ | 0 | $a_{8}, a_{7}, a_{6}[32], a_{5}, a_{4}, a_{3}, a_{2}, a_{1}$ |
| 8 | $m_{8}$ | 0 | $a_{9}, a_{8}, a_{7}, a_{6}[32], a_{5}, a_{4}, a_{3}, a_{2}$ |
| 9 | $m_{9}$ | 0 | $a_{10}, a_{9}, a_{8}, a_{7}, a_{6}[32], a_{5}, a_{4}, a_{3}$ |
| 10 | $m_{10}$ | 0 | $a_{11}, a_{10}, a_{9}, a_{8}, a_{7}, a_{6}[32], a_{5}, a_{4}$ |
| 11 | $m_{11}$ | 0 | $a_{12}, a_{11}, a_{10}, a_{9}, a_{8}, a_{7}, a_{6}[32], a_{5}$ |
| 12 | $m_{12}$ | 0 | $a_{13}, a_{12}, a_{11}, a_{10}, a_{9}, a_{8}, a_{7}, a_{6}[32]$ |
| 13 | $m_{13}$ | $2^{20}$ | $a_{14}[-21,22], a_{13}, a_{12}, a_{11}, a_{10}, a_{9}, a_{8}, a_{7}$ |
| 14 | $m_{14}$ | 0 | $a_{15}, a_{14}[-21,22], a_{13}, a_{12}, a_{11}, a_{10}, a_{9}, a_{8}$ |
| 15 | $m_{15}$ | 0 | $a_{16}, a_{15}, a_{14}[-21,22], a_{13}, a_{12}, a_{11}, a_{10}, a_{9}$ |
| 16 | $m_{16}$ | 0 | $a_{17}, a_{16}, a_{15}, a_{14}[-21,22], a_{13}, a_{12}, a_{11}, a_{10}$ |
| 17 | $m_{17}$ | $-2^{14}$ | $a_{18}[15,16,17,-18], a_{17}, a_{16}, a_{15}, a_{14}[-21,22], a_{13}, a_{12}, a_{11}$ |
| 18 | $m_{18}$ | 0 | $a_{19}, a_{18}[15,16,17,-18], a_{17}, a_{16}, a_{15}, a_{14}[-21,22], a_{13}, a_{12}$ |
| 19 | $m_{19}$ | 0 | $a_{20}, a_{19}, a_{18}[15,16,17,-18], a_{17}, a_{16}, a_{15}, a_{14}[-21,22], a_{13}$ |
| 20 | $m_{20}$ | 0 | $a_{21}, a_{20}, a_{19}, a_{18}[15,16,17,-18], a_{17}, a_{16}, a_{15}, a_{14}[-21,22]$ |
| 21 | $m_{21}$ | 0 | $a_{22}, a_{21}, a_{20}, a_{19}, a_{18}[15,16,17,-18], a_{17}, a_{16}, a_{15}$ |
| 22 | $m_{22}$ | 0 | $a_{23}, a_{22}, a_{21}, a_{20}, a_{19}, a_{18}[15,16,17,-18], a_{17}, a_{16}$ |
| 23 | $m_{23}$ | 0 | $a_{24}, a_{23}, a_{22}, a_{21}, a_{20}, a_{19}, a_{18}[15,16,17,-18], a_{17}$ |
| 24 | $m_{24}$ | $2^{10}$ | $a_{25}[11], a_{24}, a_{23}, a_{22}, a_{21}, a_{20}, a_{19}, a_{18}[15,16,17,-18]$ |
| 25 | $m_{25}$ | 0 | $a_{26}, a_{25}[11], a_{24}, a_{23}, a_{22}, a_{21}, a_{20}, a_{19}$ |
| 26 | $m_{26}$ | 0 | $a_{27}, a_{26}, a_{25}[11], a_{24}, a_{23}, a_{22}, a_{21}, a_{20}$ |
| 27 | $m_{27}$ | 0 | $a_{28}, a_{27}, a_{26}, a_{25}[11], a_{24}, a_{23}, a_{22}, a_{21}$ |
| 28 | $m_{28}$ | 0 | $a_{29}, a_{28}, a_{27}, a_{26}, a_{25}[11], a_{24}, a_{23}, a_{22}$ |
| 29 | $m_{29}$ | 0 | $a_{30}, a_{29}, a_{28}, a_{27}, a_{26}, a_{25}[11], a_{24}, a_{23}$ |
| 30 | $m_{30}$ | 0 | $a_{31}, a_{30}, a_{29}, a_{28}, a_{27}, a_{26}, a_{25}[11], a_{24}$ |
| 31 | $m_{31}$ | 0 | $a_{32}, a_{31}, a_{30}, a_{29}, a_{28}, a_{27}, a_{26}, a_{25}[11]$ |
| 32 | $m_{5}^{\prime}$ | 0 | $a_{33}, a_{32}, a_{31}, a_{30}, a_{29}, a_{28}, a_{27}, a_{26}$ |
|  |  | $\cdots$ |  |
| 94 | $m_{5}^{\prime}$ | $-2^{31}$ | $a_{95}[-32], a_{94}, a_{93}, a_{92}, a_{91}, a_{90}, a_{89}, a_{88}$ |
| 95 | $m_{2}$ | 0 | $a_{96}, a_{95}[-32], a_{94}, a_{93}, a_{92}, a_{91}, a_{90}, a_{89}$ |
| $I V_{1}^{\prime}$ |  |  | $a a_{0}, b b_{0}[32], c c_{0}, d d_{0}, e e_{0}, f f_{0}, g g_{0}, h h_{0}$ |

Table 4. A differential path for $H\left(I V_{0}, M_{0}\right)$ and $H\left(I V_{0}, M_{0}^{\prime}\right)$.

| round $i$ | $m_{i}^{\prime}$ | $\Delta a_{i+1}$ | Outputs $a_{i}^{\prime}, b_{i}^{\prime}, c_{i}^{\prime}, d_{i}^{\prime}, e_{i}^{\prime}, f_{i}^{\prime}, g_{i}^{\prime}, h_{i}^{\prime}$ |
| :---: | :---: | :---: | :---: |
| $I V_{1}^{\prime}$ |  |  | $a_{0}, b_{0}[32], c_{0}, d_{0}, e_{0}, f_{0}, g_{0}, h_{0}$ |
| 0 | $m_{0}$ | 0 | $a_{1}, a_{0}, b_{0}[32], c_{0}, d_{0}, e_{0}, f_{0}, g_{0}$ |
| 1 | $m_{1}$ | 0 | $a_{2}, a_{1}, a_{0}, b_{0}[32], c_{0}, d_{0}, e_{0}, f_{0}$ |
| 2 | $m_{2}$ | 0 | $a_{3}, a_{2}, a_{1}, a_{0}, b_{0}[32], c_{0}, d_{0}, e_{0}$ |
| 3 | $m_{3}$ | 0 | $a_{4}, a_{3}, a_{2}, a_{1}, a_{0}, b_{0}[32], c_{0}, d_{0}$ |
| 4 | $m_{4}$ | 0 | $a_{5}, a_{4}, a_{3}, a_{2}, a_{1}, a_{0}, b_{0}[32], c_{0}$ |
| 5 | $m_{5}^{\prime}$ | $2^{31}$ | $a_{6}[32], a_{5}, a_{4}, a_{3}, a_{2}, a_{1}, a_{0}, b_{0}[32]$ |
| 6 | $m_{6}$ | $2^{20}$ | $a_{7}[21], a_{6}[32], a_{5}, a_{4}, a_{3}, a_{2}, a_{1}, a_{0}$ |
| 7 | $m_{7}$ | 0 | $a_{8}, a_{7}[21], a_{6}[32], a_{5}, a_{4}, a_{3}, a_{2}, a_{1}$ |
| 8 | $m_{8}$ | $-2^{24}$ | $a_{9}[25,26,27,-28], a_{8}, a_{7}[21], a_{6}[32], a_{5}, a_{4}, a_{3}, a_{2}$ |
| 9 | $m_{9}$ | 0 | $a_{10}, a_{9}[25,26,27,-28], a_{8}, a_{7}[21], a_{6}[32], a_{5}, a_{4}, a_{3}$ |
| 10 | $m_{10}$ | $-2^{18}$ | $a_{11}[19,20,-21], a_{10}, a_{9}[25,26,27,-28], a_{8}, a_{7}[21], a_{6}[32], a_{5}, a_{4}$ |
| 11 | $m_{11}$ | 0 | $a_{12}, a_{11}[19,20,-21], a_{10}, a_{9}[25,26,27,-28], a_{8}, a_{7}[21], a_{6}[32], a_{5}$ |
| 12 | $m_{12}$ | $-2^{11}$ | $\begin{aligned} & a_{13}[12,13,14,15,16,-17], a_{12}, a_{11}[19,20,-21], a_{10}, \\ & a_{9}[25,26,27,-28], a_{8}, a_{7}[21], a_{6}[32] \end{aligned}$ |
| 13 | $m_{13}$ | $-2^{7}$ | $\begin{aligned} & a_{14}[-8], a_{13}[12,13,14,15,16,-17], a_{12}, a_{11}[19,20,-21], a_{10}, \\ & a_{9}[25,26,27,-28], a_{8}, a_{7}[21] \end{aligned}$ |
| 14 | $m_{14}$ | 0 | $\begin{aligned} & a_{15}, a_{14}[-8], a_{13}[12,13,14,15,16,-17], a_{12}, a_{11}[19,20,-21], a_{10}, \\ & a_{9}[25,26,27,-28], a_{8} \end{aligned}$ |
| 15 | $m_{15}$ | 0 | $\begin{aligned} & a_{16}, a_{15}, a_{14}[-8], a_{13}[12,13,14,15,16,-17], a_{12}, a_{11}[19,20,-21], \\ & a_{10}, a_{9}[25,26,27,-28] \end{aligned}$ |
| 16 | $m_{16}$ | 0 | $\begin{aligned} & a_{17}, a_{16}, a_{15}, a_{14}[-8], a_{13}[12,13,14,15,16,-17], a_{12}, \\ & a_{11}[19,20,-21], a_{10} \end{aligned}$ |
| 17 | $m_{17}$ | 0 | $\begin{aligned} & a_{18}, a_{17}, a_{16}, a_{15}, a_{14}[-8], a_{13}[12,13,14,15,16,-17], a_{12}, \\ & a_{11}[19,20,-21] \end{aligned}$ |
| 18 | $m_{18}$ | 0 | $a_{19}, a_{18}, a_{17}, a_{16}, a_{15}, a_{14}[-8], a_{13}[12,13,14,15,16,-17], a_{12}$ |
| 19 | $m_{19}$ | 0 | $a_{20}, a_{19}, a_{18}, a_{17}, a_{16}, a_{15}, a_{14}[-8], a_{13}[12,13,14,15,16,-17]$ |
| 20 | $m_{20}$ | 0 | $a_{21}, a_{20}, a_{19}, a_{18}, a_{17}, a_{16}, a_{15}, a_{14}[-8]$ |
| 21 | $m_{21}$ | $-2^{28}$ | $a_{22}[-29], a_{21}, a_{20}, a_{19}, a_{18}, a_{17}, a_{16}, a_{15}$ |
| 22 | $m_{22}$ | $-2^{21}$ | $a_{23}[22,23,24,-25], a_{22}[-29], a_{21}, a_{20}, a_{19}, a_{18}, a_{17}, a_{16}$ |
| 23 | $m_{23}$ | $-2^{14}$ | $\begin{aligned} & a_{24}[15,16,17,-18], a_{23}[22,23,24,-25], a_{22}[-29], a_{21}, a_{20}, a_{19}, \\ & a_{18}, a_{17} \end{aligned}$ |
| 24 | $m_{24}$ | $-2^{10}$ | $\begin{aligned} & \begin{array}{l} a_{25}[-11], a_{24}[15,16,17,-18], a_{23}[22,23,24,-25], a_{22}[-29], a_{21}, \\ a_{20}, a_{19}, a_{18} \end{array} \\ & \hline \end{aligned}$ |
| 25 | $m_{25}$ | 0 | $\begin{aligned} & a_{26}, a_{25}[-11], a_{24}[15,16,17,-18], a_{23}[22,23,24,-25], a_{22}[-29], \\ & a_{21}, a_{20}, a_{19} \end{aligned}$ |
| 26 | $m_{26}$ | 0 | $\begin{aligned} & a_{27}, a_{26}, a_{25}[-11], a_{24}[15,16,17,-18], a_{23}[22,23,24,-25], \\ & a_{22}[-29], a_{21}, a_{20} \end{aligned}$ |
| 27 | $m_{27}$ | 0 | $\begin{aligned} & a_{28}, a_{27}, a_{26}, a_{25}[-11], a_{24}[15,16,17,-18], a_{23}[22,23,24,-25], \\ & a_{22}[-29], a_{21} \end{aligned}$ |
| 28 | $m_{28}$ | 0 | $\begin{aligned} & a_{29}, a_{28}, a_{27}, a_{26}, a_{25}[-11], a_{24}[15,16,17,-18], \\ & a_{23}[22,23,24,-25], a_{22}[-29] \end{aligned}$ |
| 29 | $m_{29}$ | 0 | $\begin{aligned} & a_{30}, a_{29}, a_{28}, a_{27}, a_{26}, a_{25}[-11], a_{24}[15,16,17,-18], \\ & a_{23}[22,23,24,-25] \end{aligned}$ |
| 30 | $m_{30}$ | 0 | $a_{31}, a_{30}, a_{29}, a_{28}, a_{27}, a_{26}, a_{25}[-11], a_{24}[15,16,17,-18]$ |
| 31 | $m_{31}$ | 0 | $a_{32}, a_{31}, a_{30}, a_{29}, a_{28}, a_{27}, a_{26}, a_{25}[-11]$ |
| 32 | $m_{5}^{\prime}$ | 0 | $a_{33}, a_{32}, a_{31}, a_{30}, a_{29}, a_{28}, a_{27}, a_{26}$ |
| . $\cdot$. | $\cdots$ | $\cdots$ |  |
| 94 | $m_{5}^{\prime}$ | $\pm 2^{31}$ | $a_{95}[ \pm 32], a_{94}, a_{93}, a_{92}, a_{91}, a_{90}, a_{89}, a_{88}$ |
| 95 | $m_{2}$ | 0 | $a_{96}, a_{95}[ \pm 32], a_{94}, a_{93}, a_{92}, a_{91}, a_{90}, a_{89}$ |
| $I V_{2}^{\prime}$ |  |  | $\begin{aligned} & a_{0}+a_{96}, b_{0}[32]+a_{95}[ \pm 32], c_{0}+a_{94}, d_{0}+a_{93}, e_{0}+a_{92}, f_{0}+a_{91}, g_{0}+ \\ & a_{90}, h_{0}+a_{89} \text { Full Collision !! } \end{aligned}$ |

Table 5. A differential path for $H\left(I V_{1}, M_{1}\right)$ and $H\left(I V_{1}^{\prime}, M_{1}^{\prime}\right)$.

| round $i$ | Sufficient conditions for each round |
| :---: | :---: |
| 5 | $a_{6,32}=0$ |
| 6 | $a_{0,32}=0$ |
| 7 | $a_{2,32}=0$ |
| 8 | $a_{5,32}=a_{4,32}$ |
| 9 | $a_{7,32}=0$ |
| 10 | $a_{8,32}=1$ |
| 11 | $a_{10,32}=0$ |
| 12 | $a_{12,32}=0$ |
| 13 | $a_{14,21}=1, a_{14,22}=0$ |
| 14 | $a_{8,21}=0, a_{8,22}=0$ |
| 15 | $a_{10,21}=0, a_{10,22}=0$ |
| 16 | $a_{13,21}=a_{12,21}, a_{13,22}=a_{12,22}$ |
| 17 | $a_{18,15}=0, a_{18,16}=0, a_{18,17}=0, a_{18,18}=1, a_{15,21}=0, a_{15,22}=$ <br> $1, a_{11,22}=0, a_{12,22}=1, a_{13,22}=1, a_{16,22}=1$ |
| 18 | $a_{12,15}=0, a_{12,16}=0, a_{12,17}=0, a_{12,18}=0, a_{16,21}=1, a_{16,22}=1$ |
| 19 | $a_{14,15}=0, a_{14,16}=0, a_{14,17}=0, a_{14,18}=0, a_{18,21}=0, a_{18,22}=0$ |
| 20 | $\begin{aligned} & a_{16,15}=a_{17,15}, a_{16,16}=a_{17,16}, a_{16,17}=a_{17,17}, a_{16,18}=a_{17,18} \\ & a_{20,21}=0, a_{20,22}=0 \end{aligned}$ |
| 21 | $\begin{aligned} & a_{19,15}=0, a_{19,16}=0, a_{19,17}=1, a_{19,18}=0, a_{15,17}=1, a_{16,17}= \\ & 0, a_{17,17}=0, a_{21,17}=1 \end{aligned}$ |
| 22 | $a_{20,15}=1, a_{20,16}=1, a_{20,17}=1, a_{20,18}=1$ |
| 23 | $a_{22,15}=0, a_{22,16}=0, a_{22,17}=0, a_{22,18}=0$ |
| 24 | $a_{24,15}=0, a_{24,16}=0, a_{24,17}=0, a_{24,18}=1, a_{25,11}=0$ |
| 25 | $a_{19,11}=1, a_{20,11}=0, a_{22,11}=0, a_{21,11}=0$ |
| 26 | $a_{21,11}=0$ |
| 27 | $a_{24,11}=a_{23,11}$ |
| 28 | $a_{26,11}=0$ |
| 29 | $a_{27,11}=1$ |
| 30 | $a_{29,11}=0$ |
| 31 | $a_{31,11}=0$ |
| 94 | $a_{95,32}=1$ |
| 95 | $a_{92,32}=1$ |
| $I V_{1}$ | $a a_{0,32}=0, b b_{0,32}=0, c c_{0,32}=d d_{0,32}, f f_{0,32}=0$ |

Table 6. Sufficient conditions on $a_{i}$ for the differential path in Table 4.

| round $i$ | Sufficient conditions for each round |
| :---: | :--- |
| 0 | $f_{0,32}=0$ |
| 1 | $c_{0,32}=d_{0,32}$ |
| 2 | $a_{0,32}=0$ |
| 3 | $a_{1,32}=1$ |
| 4 | $a_{3,32}=0$ |
| 5 | $a_{5,32}=0, a_{6,32}=0$ |
| 6 | $a_{7,21}=0, a_{0,32}=0$ |
| 7 | $a_{1,21}=0, a_{2,32}=0$ |
| 8 | $a_{9,25}=0, a_{9,26}=0, a_{9,27}=0, a_{9,28}=1, a_{3,21}=0, a_{2,32}=0, a_{3,32}=$ <br> $0, a_{4,32}=1, a_{5,32}=0$ |
| 9 | $a_{7,32}=0, a_{5,21}=a_{6,21}, a_{3,25}=0, a_{3,26}=0, a_{3,27}=0, a_{3,28}=0$ |
| 10 | $a_{11,19}=0, a_{11,20}=0, a_{11,21}=1, a_{8,32}=1, a_{8,21}=0, a_{5,25}=0, a_{5,26}=$ <br> $1, a_{5,27}=0, a_{5,28}=0, a_{8,26}=0, a_{6,26}=1, a_{4,26}=0$ |
| 11 | $a_{5,19}=0, a_{5,20}=0, a_{9,21}=a_{5,21}+1, a_{7,25}=a_{8,25}, a_{7,26}=a_{8,26}, a_{8,27}=$ <br> $a_{7,27}, a_{7,28}=a_{8,28}, a_{10,32}=0$ |
| 12 | $a_{13,12}=0, a_{13,13}=0, a_{13,14}=0, a_{13,15}=0, a_{13,16}=0, a_{13,17}=1, a_{12,32}=$ <br> $0, a_{7,19}=1, a_{7,20}=0, a_{10,25}=0, a_{10,26}=0, a_{10,27}=0, a_{10,28}=0, a_{8,19}=$ <br> $1, a_{10,19}=0, a_{6,19}=0$ |
| 13 | $a_{14,8}=1, a_{7,12}=0, a_{7,13}=0, a_{7,14}=0, a_{7,15}=1, a_{7,16}=0, a_{7,17}=$ <br> $0, a_{10,19}=a_{9,19}, a_{10,20}=a_{9,20}, a_{10,21}=a_{9,21}+1, a_{11,25}=1, a_{71,26}=$ <br> 1, <br> $1, a_{11,27}=1, a_{11,28}=0, a_{7,28}=0, a_{8,28}=0, a_{8,15}=0, a_{9,15}=0, a_{10,15}=$ <br> $1, a_{11,15}=1, a_{13,21}=1$ |
| 14 | $a_{8,8}=0, a_{9,12}=0, a_{9,13}=0, a_{9,14}=0, a_{9,15}=0, a_{9,16}=0, a_{9,17}=$ <br> $1, a_{12,19}=0, a_{12,20}=0, a_{12,21}=0, a_{13,25}=0, a_{13,26}=0, a_{13,27}=0, a_{13,28}=$ <br> $0, a_{8,17}=0, a_{10,17}=0, a_{11,17}=0$ |
| 15 | $a_{10,8}=0, a_{12,12}=a_{11,12}, a_{12,13}=a_{11,13}, a_{12,14}=a_{11,14}, a_{12,15}=$ <br> $a a_{11,15}, a_{12,16}=a_{11,16}, a_{12,17}=a_{11,17}, a_{13,19}=1, a_{13,20}=1, a_{13,21}=$ <br> $1, a_{15,25}=0, a_{15,26}=0, a_{15,27}=0, a_{15,28}=0$ |
| 16 | $a_{13,8}=a_{12,8}, a_{14,12}=0, a_{14,13}=0, a_{14,14}=0, a_{14,15}=0, a_{14,16}=0, a_{14,17}=$ <br> $0, a_{15,19}=0, a_{15,20}=0, a_{15,21}=1, a_{10,21}=0, a_{12,21}=0, a_{13,21}=1, a_{14,21}=$ <br> 1 |
| 17 | $a_{15,8}=0, a_{15,12}=1, a_{15,13}=1, a_{15,14}=1, a_{15,15}=1, a_{15,16}=1, a_{15,17}=$ |
| $1, a_{17,19}=0, a_{17,20}=0, a_{17,21}=0$ |  |$|$

Table 7. Sufficient conditions on $a_{i}$ for 0-20 rounds of the differential path in Table 5.

| round $i$ | Sufficient conditions for each round |
| :---: | :--- |
| 21 | $a_{22,29}=1$ |
| 22 | $a_{23,22}=0, a_{23,23}=0, a_{23,24}=0, a_{23,25}=1, a_{16,19}=1, a_{17,29}=0$, <br> $a_{18,29}=0, a_{19,29}=0$ |
| 23 | $a_{24,15}=0, a_{24,16}=0, a_{24,17}=0, a_{24,18}=1, a_{18,29}=0, a_{17,22}=1, a_{17,23}=$ <br> $0, a_{17,24}=0, a_{17,25}=0, a_{18,22}=0, a_{19,22}=0, a_{20,22}=1, a_{21,22}=1$ |
| 24 | $a_{25,11}=1, a_{21,29}=a_{20,29}, a_{19,22}=0, a_{19,23}=0, a_{19,24}=0, a_{19,25}=$ <br> $0, a_{18,15}=0, a_{18,16}=0, a_{18,17}=0, a_{18,18}=1, a_{19,18}=0, a_{20,18}=0, a_{22,18}=$ <br> 0 |
| 25 | $a_{19,11}=0, a_{20,15}=0, a_{20,16}=0, a_{20,17}=0, a_{20,18}=0, a_{22,22}=$ <br> $a_{21,22}, a_{22,23}=a_{21,23}, a_{22,24}=a_{21,24}, a_{22,25}=a_{21,25}, a_{23,29}=0$ |
| 26 | $a_{21,11}=0, a_{23,15}=a_{22,15}, a_{23,16}=a_{22,16}, a_{23,17}=a_{22,17}, a_{23,18}=$ <br> $a_{22,18}, a_{24,22}=0, a_{24,23}=0, a_{24,24}=0, a_{24,25}=0, a_{24,29}=1$, |
| 27 | $a_{24,11}=a_{23,11}, a_{25,15}=0, a_{25,16}=0, a_{25,17}=0, a_{25,18}=0, a_{25,22}=$ <br> $1, a_{25,23}=1, a_{25,24}=1, a_{25,25}=1, a_{26,29}=0$ |
| 28 | $a_{26,11}=0, a_{26,15}=1, a_{26,16}=1, a_{26,17}=1, a_{26,18}=1, a_{27,22}=0, a_{27,23}=$ <br> $0, a_{27,24}=0, a_{27,25}=0, a_{28,29}=0$ |
| 29 | $a_{27,11}=1, a_{28,15}=0, a_{28,16}=0, a_{28,17}=0, a_{28,18}=0, a_{29,22}=0, a_{29,23}=$ <br> $0, a_{29,24}=0, a_{24,25}=0, a_{25,25}=1, a_{27,25}=0, a_{29,25}=1$ |
| 30 | $a_{29,11}=0, a_{30,15}=0, a_{30,16}=0, a_{30,17}=0, a_{30,18}=1, a_{25,18}=0, a_{26,18}=$ <br> $1, a_{28,18}=0$ |
| 31 | $a_{31,11}=1, a_{26,11}=0, a_{27,11}=1, a_{29,11}=0$ |
| 95 | $a_{92,32=1}=1$ |

Table 8. Sufficient conditions on $a_{i}$ for 21-95 rounds of the differential path in Table 5.


[^0]:    ${ }^{3}$ The newest version is HAVAL 1.1. We can download the program source code at the website [1]. The difference between the first version and HAVAL 1.1 is only the order of initial values and the other constant values.

[^1]:    ${ }^{4}$ Our differential is used in an attack on 4-pass HAVAL by H.Yu et al. [7], but it is new for 3 -pass HAVAL.

[^2]:    ${ }^{5}$ The operation + is the word-wise modular $2^{32}$ addition.
    ${ }^{6}$ This differential was used for 4-pass HAVAL [7]. Its complexity is $2^{43}$.
    ${ }^{7}$ Table 4 was given in [7]. We constructed Table 5.

[^3]:    ${ }^{8}$ Note that our algorithm doesn't requre message modification.

[^4]:    ${ }^{9}$ It takes about one minute on our computer.

