A Practical Chosen Message Power Analysis Approach against the Key Whitening Layers on the Loop Architecture

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Abstract. In practice, the key whitening layer is a commonly adopted structure in symmetric ciphers, and the loop architecture is widely applied in hardware implementation of these ciphers. Up to now, conventional DPA is hard to recover the key of such ciphers, since the key whitening layer hides the input (output) of the first (last) round from the plaintext (ciphertext). In this paper, we propose a practical chosen message power analysis approach against the loop architecture of ciphers with the key whitening layers. The starting point of the new approach is the delicate selection of the plaintext set in a chosen message manner, which decreases the space of the plaintext to a reasonable size within the ability of DPA. After choosing the plaintext, we can recover the whitening key through fully exploiting the intermediate variable which is mixed up with the round key and the whitening key. More precisely, we take the round key and the whitening key as a unity and recover it by the chosen message DPA, and then derive the whitening key according to the relationship between the whitening key and the unity. Finally, we can derive the master key from the whitening keys. In order to further manifest the validity of the new approach, we carry extensive experiments on two ISO standardized ciphers CLEFIA and Camellia implemented in loop architecture on FPGA, and the keys are recovered as expected.

Keywords: DPA, key whitening, chosen message, loop architecture, FPGA

1 Introduction

The hardware implementations of ciphers usually follow two architectures, compact architecture and loop architecture [19], in order to adapt to different application scenarios. In the embedded application scenario, the size, power consumption, and cost of the cryptographic device are tightly restrained. On the other hand, in the higher computation speed and higher throughput application
scenario, the performance and efficiency of the cryptographic device are the most important indicators. The compact architecture usually takes several clock cycles to accomplish a single round computation of the cryptographic algorithm, such as reusing the single substitution circuit (e.g., Sbox) several times as a subloop instead of using their duplications concurrently. Therefore, the compact architecture, which sacrifices performance to less circuit components, is often applied to the embedded cryptographic device, such as smart cards and wireless sensor nodes. On the other hand, the loop architecture defines the round function of the cryptographic algorithm as several consecutive operations, which means that a single round is computed in one clock cycle. Compared to the compact architecture, the loop architecture, which has higher throughput or less calculation time, is usually applied to the higher computation speed and higher throughput application scenario, such as the hardware security module in the cloud computing environment, the instant messenger system, the network authentication system and the network routing device. The loop architecture is implemented in ASIC or FPGA chips in the hardware security module, with the advancement of circuit industry within recent years. With the increase in the number of the hardware security module using the loop architecture, the capability of the loop implementation against the side channel attack has attracted researchers’ great attention.

Since first proposed by Kocher et al. in [1], DPA has proven to be a powerful method of side channel attack against many ciphers within these years. Normally, DPA can only deal with a small fraction of the long secret key (e.g., several round key bits) through a divide-and-conquer strategy, and its validity is highly dependent on the specific implementing method. According to the relatively small size (8-bit or less) of subkey mixed up in the available intermediate variable, these compact implementations are easily compromised by the conventional DPA, where the possible input space of random test vector is only $2^8$ or less [18]. For instance, DES, AES and many other ciphers under the compact architecture have shown to be vulnerable against DPA [1, 4, 11, 13, 14].

In spite of successfully dealing with the loop architecture, the conventional DPA is not as efficient and feasible as the chosen message DPA. The adversary has to collect much more power traces (e.g., several million traces or more) to launch the conventional DPA against the loop architecture, in order to reveal the large size of subkey fraction (e.g., 32-bit or more). It leads to that the conventional DPA against the loop implementations of ciphers is unpractical. The work in [16] shows that the conventional DPA solves the problem of large key space with very high complexity. On the contrary, chosen message DPA proposed in [15] can decrease the size of the available intermediate variable to a practically small size (8-bit or less), and thus requires only a small number of power traces and very few computational efforts.

Both the conventional DPA and the chosen message DPA would only work with the known message assumption. However, in order to enhance the security properties of the ciphers, the key whitening layers are generally performed before the first round and after the last round, thus hiding the input (output) of the
first (last) round from the plaintext (ciphertext). Therefore, the key whitening
operations seem to contradict the basic requirements of the DPA methodology.
Fortunately, the key whitening layers are also easily compromised by DPA in the
compact, through directly analyzing the power consumption of the whitening op-
eration (e.g. XOR) on power traces [12]. It is caused by the implementation of
the key whitening layers in the compact architecture. In the compact architec-
ture where the cipher has the key whitening layer, the key whitening layer is
implemented independently of the substitution circuit.

However, it is quite a challenge to launch the DPA methodology against
the loop hardware implementations of ciphers with the key whitening layers. In
contrast to the compact case, the key whitening layer is usually implemented
with the first or last round in the loop architecture, which can increase the
difficulty of the DPA methodology. The reasons are as follows: Firstly, the power
consumption of the whitening operation is hard to detect from power traces,
because the intermediate result of the whitening operation does not appear in
registers or on bus. Secondly, the whitening key is difficult to be separated from
the round key and other intermediate variables by DPA. More precisely, the
attacker can only get the equivalent key (i.e. the value of “the round key adding
the whitening key” as a unity) in DPA with a chosen message manner, but he
would not be capable to directly determine the values of the whitening key and
the round key. Consequently, launching the attack under the influence of the key
whitening layers, is an interesting challenge.

**Our Contributions.** In this paper, we propose a practical chosen message
power analysis method on loop architecture of ciphers with the key whitening
layers. We focus on the Feistel-SP ciphers with the key whitening layers, due to
the most comprehensive cases of the key whitening layers in these ciphers (i.e.,
the key whitening operation on the left branch, on the right branch, and on
both branches). Our contributions can be briefly summarized from the following
aspects:

– **We propose a practical chosen message DPA approach to recov-
er the whitening key through a divide-and-conquer strategy.** Our
approach can fully exploit the relationship between the round key and the
whitening key in the round function. According to the relationship in the
round function, our approach can launch DPA to reveal the whitening key,
by selecting the plaintext set in a chosen message manner similar to the
traditional cryptanalysis against byte-oriented ciphers. When the whitening
key is on the left branch of Feistel-SP ciphers, we can efficiently recover the
whitening key. When the whitening key is on the right branch, we are able
to reduce the recovery of the whitening key on the right branch to the left
branch case through an adaptive chosen message manner. Therefore, if there
are whitening keys on both branches, we can recover the whitening keys for
each branch alternately.
We perform extensive experiments on two ISO standardized ciphers CLEFIA and Camellia with loop FPGA implementations. Experimental results show that all bits of the keys in both ciphers can be recovered as expected.

Structure. The remainder of this paper is organized as follows. In Section 2, the preliminaries are briefly described. Section 3 illustrates the practical chosen message power analysis method on Feistel-SP ciphers with the key whitening layers. Section 4 elaborates the practical attacks on two loop FPGA implementations of CLEFIA-128 and Camellia-128 in order to prove the effectiveness of our approach. We discuss and summarize the paper in Section 5.

2 Preliminaries

2.1 Feistel-SP structure

The Feistel network is one of the most famous architectures in symmetric cryptography. According to the classifications of [5], the Feistel network has several derivatives, namely, the unbalanced Feistel network [6], the alternating Feistel network [8, 9], the numeric Feistel network, and the famous type-1, type-2, and type-3 Feistel networks [10]. Many practical block ciphers utilize the Feistel networks including DES (plain), Skipjack (unbalanced), BEAR/LION (alternating), CAST (type-1), CLEFIA (type-2) and MARS (type-3).

A typical SP type function often consists of three operations, i.e., subkey addition, substitution, and permutation. In the subkey addition, a subkey is XORed to the state. The substitution is applied by Sbox-like non-linear bijection. In the permutation, a linear bijection (generally an MDS multiplication) is performed. Let \( S_1, S_2, \ldots, S_t : \{0,1\}^s \rightarrow \{0,1\}^s \) be non-linear bijections, \( P : \{0,1\}^{st} \rightarrow \{0,1\}^{st} \) be a linear bijection, \( k = (k_1, k_2, \ldots, k_t) \) is the round key, then the round function \( F : \{0,1\}^{st} \times \{0,1\}^{st} \rightarrow \{0,1\}^{st} \) of SP type is defined by \( F(x, k) = P(S_1(x_1 \oplus k_1), S_2(x_2 \oplus k_2), \ldots, S_t(x_t \oplus k_t)) \). The notations \( s \) and \( t \) represent the size of the non-linear bijection and the number of the non-linear bijections, respectively.

In the Feistel network, the core of the underlying round function is referred to as the F-function. In order to combine the advantages of SPN structures, the Feistel-SP ciphers use well-designed SPN functions as the F-functions. The typical round function of the Feistel-SP structure is shown in Fig.1.

2.2 DPA on the Key Whitening Layer

Key whitening is a technique intended to enhance the strength of a block cipher by adding key-relevant operations before the first round and after the last round without major changes in the algorithm. It consists of steps that combine the data with portions of the key before the first round and after the last round. The most common form of operation is XORing or modular adding the whitening key.
to the plaintext/ciphertext. In the compact architecture where the cipher has the key whitening layer, the key whitening layer is implemented independently of the substitution circuit. On the contrary, the key whitening layer is usually implemented with the first or last round in the loop architecture.

The key whitening layers can be easily compromised by DPA, if attackers are able to capture the power consumption of the whitening operation on power traces. In the compact scenario, due to the independent implementation of the key whitening layer, the power consumption of the whitening operation is convenient to be observed, and attackers can reveal the whitening key through direct analysis of the power consumption of the whitening operation [12]. Unfortunately, the above strategy seems hard to apply in the loop scenario, which implements the whitening operations into the first or last round, mainly because of the slight power consumption which is too difficult to be detected. Therefore, we propose a practical chosen message DPA approach to recover the whitening key in the loop scenario, and more details will be discussed in Section 3.3 and 3.4.

3 The Design of Our Approach

In this section, we describe the details of our practical chosen message DPA method on the loop architecture of Feistel-SP ciphers with the key whitening layers. Firstly, sharing the similar idea on the case of AES-256 in [15], we put forward the chosen message manner which is suitable for the case of Feistel-SP ciphers without the key whitening layers. Secondly, we analyze the difficulty to reveal the whitening key in the loop architecture directly. Then we propose an efficient approach to recover the whitening key through a divide-and-conquer strategy. More precisely, we show how to recover the whitening key on the left branch, and reduce the recovery of the whitening key on the right branch to the left branch case through an adaptive chosen message manner. Combining these two strategies, we manage to perform practical DPA on loop architecture of Feistel-SP ciphers with the key whitening layers.
3.1 The Chosen Message DPA on the Loop Architecture of Feistel-SP

The typical loop implementation of Feistel-SP cipher is shown in Fig.1. Let $L_i$ and $R_i$ denote the left and right branches of the $i$-th round input respectively, and the size of the Sbox is 8-bit. The right branch $R_i$ can be further split into $t$ 8-bit cells, namely, $R_i = x_1 || x_2 || \cdots || x_t$. Each 8-bit cell $x_j$ is first XORed with the corresponding 8-bit round key $r_{kj}$, then all $t$ cells are processed with $t$ parallel Sboxes $S_1, S_2, \cdots, S_t$. Let $y_1 || y_2 || \cdots || y_t$ denote the output of the Sbox layer, the linear permutation $P$ (normally multiplication with an MDS matrix) updates the state $y_1 || y_2 || \cdots || y_t$, and $z_1 || z_2 || \cdots || z_t$ is the output. The right branch of the $i$-th round output $R_{i+1}$ is then calculated by XORing $L_i$ and the output of $P$, while the left branch $L_{i+1}$ is updated by directly assigning the value of $R_i$. The above procedures can be described as

\[
L_{i+1} = R_i,
\]
\[
R_{i+1} = F(R_i, r_k) \oplus L_i
= P(S_1(x_1 \oplus r_{k1}), S_2(x_2 \oplus r_{k_2}), \cdots, S_t(x_t \oplus r_{k_t})) \oplus L_i. \tag{1}
\]

In the scenarios of compact implementations, the 8-bit intermediate value $y_j = S_j(x_j \oplus r_{kj})$, is calculated sequentially, and arise on bus from the MOV instruction or store into registers, thus becomes a DPA attacking point as shown in Fig.2(a). However, the loop architecture of Feistel-SP treats the round function as several consecutive operations, thus no intermediate result except $R_{i+1}$ is written into registers in the loop implementations. The power consumption of $y_j$ is much less than $R_{i+1}$ and hard to be observed. Therefore, in loop implementations, we are only able to attack at this point when the data $R_{i+1}$ is being written into registers as shown in Fig.2(b).

However, traditional DPA with random message is not suitable for $R_{i+1}$ due to the large size of the intermediate variable. More specifically, the intermediate variable is calculated through the whole round operation, and thus entangled with all the round key bits (32 bits or more). In order to significantly decrease the size of the target intermediate variable to a practically small size (8-bit or less), we apply the chosen message DPA.

As shown in Fig.2(b), regarding a specific cell $y_j$, the linear permutation $P$ can be represented as follows:

\[
P(y_1, y_2, \cdots, y_{j-1}, y_j, y_{j+1}, \cdots, y_t) = P(0, 0, \cdots, 0, y_j, 0, \cdots, 0) \oplus P(y_1, y_2, \cdots, y_{j-1}, 0, y_{j+1}, \cdots, y_t)
= WP^j \oplus CP^j,
\]

where the superscript $j$ indicates the function focusing on the cell $y_j$, and $WP^j$ and $CP^j$ denote the two components of the right half of the equation respectively. The above equation can be rewritten in byte-wise form as follows:

\[
P_{[1]} || P_{[2]} || \cdots || P_{[t]} = (WP^j_{[1]} || WP^j_{[2]} || \cdots || WP^j_{[t]}) \oplus (CP^j_{[1]} || CP^j_{[2]} || \cdots || CP^j_{[t]})
\]

\footnote{The Sboxes can be identical or distinct.}
where the subscript \([k]\) indicates the \(k\)-th byte output, and \(WP^j_{[k]}\) and \(CP^j_{[k]}\) denote the \(k\)-th bytes of \(WP^j\) and \(CP^j\) respectively. If we fix the values of all \(y_k\) where \(k \neq j\), and keep \(y_j\) as a variable, then \(WP^j_{[j]}\) can be seen as a function of \(y_j\) and \(CP^j_{[j]}\) is a constant. For convenience, we use \(P'_{[j]}\) and \(mask_{[j]}\) to represent \(WP^j_{[j]}\) and \(CP^j_{[j]}\) respectively.

Thus, attackers choose the specific byte of plaintext message, which corresponds the \(j\)-th byte of the target intermediate variable, while fixing other bytes of the plaintext message. The target byte is dependant on two unknown constant one-byte parameters, \(i.e.,\) the subkey \(rk_j\) and the \(mask_{[j]}\) generated by \(P\). Therefore, the size of guessed parameters from the whole round key is decreased to a pair of 8-bit values, \(i.e.,\) the hypothesis space of the secret value falls to \(2^{16}\), and the input space of the plaintext message is decreased to \(2^8\), which is suitable for practical DPA. Consequently, by alternately choosing the corresponding plaintext message byte for all possible positions, we can use the DPA attacking model shown in Fig.3 to launch DPA and recover all \(t\) bytes of the round key (for the sake of simplicity, we assume the size of the round key is 32 bits).

3.2 The Difficulty to Reveal The Whitening Key in the Loop Scenario

The whitening keys are generally used before the first round and after the last round. After the key whitening operations, the inputs (outputs) to the first (last) round are covered by the unknown whitening key from the plaintexts (ciphertexts). It seems that such operations would increase the size of unknown parameters and make the attack more difficult. However, through detailed analysis, we find that the Whitening Key Reveal (WKR) scenario can still be attacked effectively.

Fig. 2. Different DPA attack points of Feistel-SP (a) Compact (b) Loop
parameters, and raise the difficulty to launch a DPA attack. However, since the encryption and decryption of Feistel-SP ciphers follow similar procedures and both the pre-whitening and the post-whitening keys are almost equivalent from the perspective of DPA, we only discuss the encryption procedure in the first round.

Let $ML$ (resp. $MR$) denote the left (resp. right) message branch, and $wkL$ (resp. $wkR$) denote the left (resp. right) whitening key. As shown in Fig.4, the whitening keys can be applied on the left branch, the right branch or both branches, which correspond to three types of whitening operations.

There are two main difficulties to apply DPA to reveal the whitening key in loop scenario. The first difficulty is that the power consumption of the whitening operation is hard to detect from power traces similar as Section 3.1. In the loop hardware implementation, the whitening operation and the round key addition operation are usually combined as one operation (i.e. $Message \oplus wk \oplus rk$), which is implemented by 3-input XOR gate or LUT. More precisely, there is no standalone whitening operation in the Feistel-SP computing procedure, thus the

![Fig. 3. DPA model of Feistel-SP in loop scenario](image)

![Fig. 4. The whitening key on (a) left branch (b) right branch (c) both branches](image)
power consumption of the whitening operation is hard to detect. Therefore, the existing method against the whitening key as mentioned in [12] is not suitable.

Moreover, although we could choose $R_{i+1}$ as the attack point, the whitening key is difficult to be separated from the round key and other intermediate variables by DPA. We assume that there are whitening keys on both branches. Due to the effect of whitening keys $wkL$ and $wkR$, the DPA attacking model of Feistel-SP with whitening key in loop scenario is shown in Fig.5(a). For the loop scenario, we use $rk \oplus wkR$ as the equivalent key and $mask \oplus wkL$ as the equivalent mask, thus the model is changed from Fig.5(a) to Fig.5(b). However, although we can recover the equivalent key and the equivalent mask by DPA, we are unable to directly determine the values of the whitening keys from the equivalent key and the equivalent mask.

![Diagram](image)

**Fig. 5.** Chosen Message DPA model of Feistel-SP whitening key in the loop scenario

### 3.3 Recovery of $wkL$

When we choose $R_{i+1}$ as the attack point, the main drawback for DPA is the difficulty to separate the whitening key from the equivalent key and the equivalent mask. Luckily, we can achieve this goal through the divide-and-conquer strategy. More precisely, we can efficiently recover the whitening key on the left branch $wkL$, and the recovery of the whitening key on the right branch can be reduced to the left branch case.

The recovery of $wkL$ is based on the full exploitation of the complex relationship between the equivalent key and the equivalent mask with a chosen message DPA method. Hereafter we use subscript $[i]$ ($1 \leq i \leq t$) to indicate the $i$-th byte of the corresponding variable or the output of one function, and use notation $rk_{j}$ ($j \geq 1$) to represent the round key in the $j$-th round of Feistel-SP ciphers. According to Fig.4(a), two branches of the first round input $L_1||R_1$ can
be described by:

$$L_1 || R_1 = (ML \oplus wkL) || MR.$$  \hspace{1cm} (2)

Now, we will focus on the attack point $R_2$ as shown in Fig. 2. Equation 1 can be rewritten as:

$$R_2 = F(R_1, rk_1) \oplus L_1$$
$$= P(S_1(MR_{[1]} \oplus rk_{1,[1]}), S_2(MR_{[2]} \oplus rk_{1,[2]}),$$
$$\ldots, S_t(MR_{[t]} \oplus rk_{1,[t]})) \oplus wkL \oplus ML.$$  \hspace{1cm} (3)

where $MR = MR_{[1]} || MR_{[2]} || \cdots || MR_{[t]}$, and $rk_1 = rk_{1,[1]}$

$||rk_{1,[2]}|| \cdots ||rk_{1,[t]}||$

We focus on the first byte of $R_2$, and fix all $MR_{[j]}$ ($2 \leq j \leq t$) to constants, that leads to the constant output of $S_j$. Thus, Equation 3 can be rewritten in byte-wise form:

$$R_{2,[1]} = F_{[1]}(R_{1,[1]} \oplus L_{1,[1]}$$
$$= P_{[1]}(S_1(MR_{[1]} \oplus rk_{1,[1]}), S_2(MR_{[2]} \oplus rk_{1,[2]}),$$
$$\ldots, S_t(MR_{[t]} \oplus rk_{1,[t]})) \oplus wkL_{[1]} \oplus ML$$
$$= P_{[1]}'(S_1(MR_{[1]} \oplus rk_{1,[1]})) \oplus mask_{1,[1]} \oplus wkL_{[1]} \oplus ML$$
$$= P_{[1]}'(S_1(MR_{[1]} \oplus rk_{1,[1]})) \oplus mask_{1,[1]} \oplus ML.$$  \hspace{1cm} (4)

with $ML = ML_{[1]} || ML_{[2]} || \cdots || ML_{[t]}$, $wkL = wkL_{[1]} || wkL_{[2]}$

$|| \cdots || wkL_{[t]}$. Moreover, $mask_{1} = mask_{1,[1]} || mask_{1,[2]} || \cdots \|$ $mask_{1,[t]}$ is the intermediate variable which is generated in the first round. According to Section 3.1, $mask_{1,[j]}$ is a byte constant value if all $MR_k$ ($k \neq j$) are fixed since the round key $rk_1$ have already been prefixed, and the equivalent mask $MASK_1 = mask_{1} \oplus wkL$.

At this time, $R_{2,[1]}$ is highly related to $rk_{1,[1]}$, and $R_{2,[2]}, R_{2,[3]}, \ldots, R_{2,[t]}$ will be treated as noise. Now, we can launch DPA against $R_{2,[1]}$ by enumerating 8-bit $MR_{[1]}$ while fixing other bits of $MR$ and $ML$. Thus, both 8-bit $rk_{1,[1]}$ and 8-bit $MASK_{1,[1]}$ are revealed by DPA, where the possible hypotheses space is $2^{16}$ and the possible input space of random test vector $MR_{[1]}$ is only $2^8$. With the same approach, we could analyze $R_{2,[2]}, R_{2,[3]}, \ldots, R_{2,[t]}$ byte by byte, and reveal the values of $rk_{1,[2]}, rk_{1,[3]}, \ldots, rk_{1,[t]}$ and $MASK_{1,[2]}, MASK_{1,[3]}, \ldots, MASK_{1,[t]}$.

According to the complex relationship between $rk_1$ and $mask_{1,[j]}$, we could iteratively calculate each of $mask_{1,[j]}$ by all bytes of $rk_1$. More precisely, according to Equation 4, $mask_{1,[1]}$ is calculated by:

$$mask_{1,[1]} = P_{[1]}'(S_1(MR_{[1]} \oplus rk_{1,[1]})) \oplus P_{[1]}(S_1(MR_{[1]} \oplus rk_{1,[1]}),$$
$$S_2(MR_{[2]} \oplus rk_{1,[2]}), \ldots, S_t(MR_{[t]} \oplus rk_{1,[t]})).$$  \hspace{1cm} (5)

$mask_{1,[j]}$ ($j \in [2, t]$) is calculated similarly. Then the values of all $wkL_{[k]}$ ($k \in [1, t]$) is iteratively calculated by $wkL_{[k]} = MASK_{1,[k]} \oplus mask_{1,[k]}$. Thus, the whitening key $wkL$ is recovered, and our method is suitable for launching DPA to recover the whitening key on the left branch of Feistel-SP in loop architecture.
3.4 Recovery of \( wkR \)

According to Section 3.3, we reveal the round key \( rk_1 \) and the equivalent mask \( MASK_1 \) in the first round, and then successfully derive the left branch whitening key \( wkL \) from above two parameters. However, due to Fig.4(b) and Fig.5, the right branch whitening key \( wkR \) is hard to be distinguished from the equivalent key, because both \( wkR \) and \( rk_1 \) have exactly the same effects on the SP type F-function in the first round of Feistel-SP ciphers. More precisely, according to Equation 4, the first byte of \( F \)-function in the first round of Feistel-SP ciphers. More precisely, according to Equation 4, the first byte of \( F \)-function in the first round of Feistel-SP ciphers. More precisely, according to Equation 4, the first byte of \( F \)-function in the first round of Feistel-SP ciphers. More precisely, according to Equation 4, the first byte of \( F \)-function in the first round of Feistel-SP ciphers. More precisely, according to Equation 4, the first byte of \( F \)-function in the first round of Feistel-SP ciphers.

\[
R_{2,1} = F_{1}(R_1, rk_1) \oplus L_{1,1}
\]
\[
= P_{1}(S_1(MR_{1} \oplus wkR_{1} \oplus rk_{1,1}), S_2(MR_{2} \oplus wkR_{2} \oplus rk_{1,2}), \cdots, S_t(MR_{t} \oplus wkR_{t} \oplus rk_{1,t})) \oplus ML_{[1} \\
= P_{1}(S_1(MR_{1} \oplus wkR_{1} \oplus rk_{1,1})) \oplus mask_{1,[1]} \oplus ML_{[1}.
\]

with \( wkR = wkR_{1}||wkR_{2}||\cdots||wkR_{[t]} \) and the equivalent key \( ek_{1} = rk_{1} \oplus wkR \) and \( mask_{1,[1]} \) is a byte constant value if \( MR_{[2]}, MR_{[3]}, \cdots, MR_{[t]} \) are fixed since the equivalent key \( ek_{1} \) have already been prefixed. In this scenario, we can only reveal each byte of \( ek_{1} \) and \( mask_{1} \) with the approach proposed in Section 3.3, and we are unable to split \( wkR \) from \( ek_{1} \).

Therefore, we have to find relations between the case of the whitening key on the right branch and the case of the whitening key on the left branch in order to recover \( wkR \). We focus on the second round of Feistel-SP. As shown in Fig.6(a), the whitening key \( wkR \) is mixed up with \( mask_{2} \) in the second round of Feistel-SP, and we choose \( R_{3} \) as the attack point in the second round. Equation 3 and Equation 4 can be rewritten as:

\[
R_3 = F(R_2, rk_2) \oplus L_2
\]
\[
= P(S_1(R_{2,1} \oplus rk_{2,1}), S_2(R_{2,2} \oplus rk_{2,2}), \cdots, S_t(R_{2,[t]} \oplus rk_{2,[t]})) \oplus wkR \oplus MR.
\]

\[
R_{3,1} = F_{1}(R_2, rk_2) \oplus L_{2,1}
\]
\[
= P_{1}(S_1(R_{2,1} \oplus rk_{2,1}), S_2(R_{2,2} \oplus rk_{2,2}), \cdots, S_t(R_{2,[t]} \oplus rk_{2,[t]})) \oplus wkR_{[1]} \oplus MR_{[1]} \\
= P_{1}(S_1(R_{2,1} \oplus rk_{2,1})) \oplus mask_{2,[1]} \oplus wkR_{[1]} \oplus MR_{[1]} \\
= P_{1}(S_1(R_{2,1} \oplus rk_{2,1})) \oplus MASK_{2,[1]} \oplus MR_{[1]}.
\]

where \( mask_{2,[1]} \) is a byte constant value if \( R_{2,2}, R_{2,3}, \cdots, R_{2,[t]} \) are fixed since the round key \( rk_{2} \) have already been prefixed. Therefore, as shown in Fig.6(b), if we can control the input of the second round \( L_{2,1}||R_{2} \) as the plaintext message \( ML_{[1]}||MR \), we will reduce the case of the whitening key on the right branch in the second round to the case of the whitening key on the left branch in the first round.
Fortunately, we can control the input of the second round $L_2||R_2$ in an adaptive chosen message manner. Firstly, we reveal $e_k_1$ in the first round. Then based on the values of $L_2||R_2$ which meets the chosen message requirements, we calculate the corresponding plaintext message with $e_k_1$ through the inverse transformation of the Feistel-SP round function. Finally, we could establish the chosen plaintext set which is suitable for the second round and reduce the case of $wkR$ to the case of $wkL$, and reveal $wkR$ for the second round of Feistel-SP.

On Recovering the Whitening Keys on Both Branches. Our approach is also suitable for Feistel-SP ciphers with the key whitening layer on both branches, as shown in Fig.4(c). The specific procedures of this scenario are as follows:

- **Step 1. Reveal the Whitening Key $wkL$ in the First Round.** The first step of our method is to reveal $wkL$ in the first round. We establish the chosen plaintext set which enumerates all possible values of the target bytes ($MR_1$), and fixes other bytes to constants. Then, we repeat the DPA attack against $R_2$ several times to recover all bytes of $e_k_1$ and $MASK_1$. Finally, we calculate $mask_1$ by $e_k_1$ and reveal $wkL$ with the equation $wkL = MASK_1 \oplus mask_1$.

- **Step 2. Reveal the Whitening Key $wkR$ in the Second Round.** The second step of our method is to establish the chosen plaintext set which is used for the second round, through an adaptive chosen message manner. According to Section 3.4, it can be done with similar strategy of Step 1 to recover $wkR$.

4 Applications

We apply these techniques to two typical Feistel-SP ciphers, CLEFIA-128 [2] and Camellia-128 [3], to verify the effectiveness of our method. We implement both...
ciphers with the loop architecture on a Virtex-5 Xilinx FPGA on SASEBO-GII board. Pearson Correlation Coefficient based Power Analysis (CPA) is applied during the security analysis. The aim is to recover the master keys in CLEFIA-128 and Camellia-128, and the master keys are recovered as expected in both experiments, thus manifesting the correctness of our approach.

4.1 Application to CLEFIA-128

Specification of CLEFIA-128. CLEFIA-128 is a type-2 Feistel-SP cipher proposed at FSE 2007 by Shirai et al. It is standardized by ISO [20] as a lightweight cipher. It encrypts a 128-bit plaintext into a 128-bit ciphertext with a 128-bit master key after applying the round function 18 times, as shown in Fig.7.

Let $P$ and $K$ be the 128-bit plaintext and the master key respectively. Thirty-six 32-bit round keys $r k_0, r k_1, \ldots, r k_{35}$ and four 32-bit whitening keys $w k_0, w k_1, w k_2, w k_3$ are generated from $K$. These whitening keys are defined as $w k_0 || w k_1 || w k_2 || w k_3 = K$ according to the key schedule.

Let $X^i_0 || X^i_1 || X^i_2 || X^i_3 (0 \leq i \leq 17)$ be an internal input state in each round. The plaintext is loaded into $P^i_0 || P^i_1 || P^i_2 || P^i_3$. Next, $X^i_0$ and $X^i_2$ are updated by the pre-whitening layer, that is $(X^i_0, X^i_1, X^i_2, X^i_3) = (P^i_0 \oplus w k_0, P^i_1, P^i_2 \oplus w k_1)$. Then, the internal state is updated by the following computation up to the second last round (for $1 \leq i \leq 17$);

$$
X^i_0 = X^{i-1}_1 \oplus F_0(X^{i-1}_0, r k_{2i-2}), \quad X^i_1 = X^{i-1}_2,
$$

$$
X^i_2 = X^{i-1}_3 \oplus F_1(X^{i-1}_2, r k_{2i-1}), \quad X^i_3 = X^{i-1}_0.
$$

Two SP type F-functions $F_0$ and $F_1$ consist of a 32-bit round key addition, an S-box transformation, and a multiplication by an MDS matrix, as shown in Fig.8.
Four parallel 8-bit Sboxes are applied, followed with an MDS multiplication in each of SP type F-functions. In addition, the MDS matrices for two SP type F-functions are different.

In the last round, \( X_{18}^0 || X_{18}^1 || X_{18}^2 || X_{18}^3 \) is computed by

\[
X_0^{18} = X_0^{17}, \quad X_1^{18} = X_1^{17} \oplus F_0(X_0^{17}, r k_{34}), \\
X_2^{18} = X_2^{17}, \quad X_3^{18} = X_3^{17} \oplus F_1(X_2^{17}, r k_{35}).
\]

Finally, \( C_1 \) and \( C_3 \) are updated by the post-whitening layer, i.e., \((C_0, C_1, C_2, C_3) = (X_0^{18}, X_1^{18} \oplus w k_2, X_2^{18}, X_3^{18} \oplus w k_3)\), and \( C_0 || C_1 || C_2 || C_3 \) is the final ciphertext.

**Attack of CLEFIA-128.** CLEFIA adopts 4-branch Type-2 Feistel network but uses two different diffusion matrices for the diffusion switching mechanism. It has the key whitening layer and only the left branch of the plaintext blocks is XORed with the whitening key. Our aim is to reveal the master keys through the recovery of the whitening keys.

Hereafter we use the notations \( P_j \) and \( C_j \) for CLEFIA-128 to represent the plaintext and ciphertext in the \( j \)th branch, \( X_j^i \) to represent the state in the \( j \)th branch immediately after the round operation in round \( i \), \( X_j^0 \) to represent the output of the key whitening layer before the first round. We use the notations \( F_0, F_1, S_0, S_1, M_0 \), and \( M_1 \) to further distinguish the different round functions of CLEFIA-128. The subscript \([n]\) indicates the \( n \)th byte of the state.

To reveal the master key \( K \) of CLEFIA-128, we focus on the whitening key. As shown in Fig.7, the four 32-bit whitening keys \( w k_0, w k_1, w k_2, w k_3 \) are generated from \( K \). These whitening keys are defined as \( w k_0 || w k_1 || w k_2 || w k_3 = K \). Thus, we do not need to calculate the inverse transformation of CLEFIA key schedule to reveal \( K \), if we get the whitening key value. There are two key whitening layers in CLEFIA-128, the pre-whitening before the first round and the post-whitening after the last round. According to the Section 3.3, CLEFIA-128 belongs to the case of the whitening key on the left branch. Hence, our attack target is the first round and the last round of CLEFIA-128.

In order to recover both the pre-whitening and the post-whitening keys, the attack should be conducted in both the encryption and the decryption directions.
respectively. However, since the encryption and decryption of CLEFIA follow similar procedures and $F_0$ and $F_1$ are almost equivalent from the perspective of DPA, the attack procedures for recovering the whitening keys are almost identical. Thus we only describe the detailed process to recover $wk_0$.

The whitening key $wk_0$ is only XORed with 32-bit plaintext block $P_1$, and $rk_0$ is the round key. According to the specification of CLEFIA-128 and Equation.1, the 32-bit output $X_0^1$ is described by

$$X_0^1 = F_0(X_0^0, rk_0) \oplus X_1^0$$
$$= M_0(S_0(P_{0,[1]} \oplus rk_{0,[1]}), S_1(P_{0,[2]} \oplus rk_{0,[2]}), \cdots , S_1(P_{0,[4]} \oplus rk_{0,[4]})) \oplus wk_0 \oplus P_1. \quad (9)$$

Focusing on the first byte of $X_0^1$, Equation.9 could be rewritten as

$$X_{0,[1]}^1 = S_0(P_{0,[1]} \oplus rk_{0,[1]}) \oplus mask_{0,[1]} \oplus wk_{0,[1]} \oplus P_{1,[1]}$$
$$= S_0(P_{0,[1]} \oplus rk_{0,[1]}) \oplus MASK_{0,[1]} \oplus P_{1,[1]}, \quad (10)$$

where $mask_{0,[1]}$ is generated by $S_1(P_{0,[2]} \oplus rk_{0,[2]}), S_0(P_{0,[3]} \oplus rk_{0,[3]}),$ and $S_1(P_{0,[4]} \oplus rk_{0,[4]}),$ and $MASK_0$ is defined as $MASK_0 = mask_0 \oplus wk_0$.

Therefore, we can reveal the values of $rk_0$ and $MASK_0$ by chosen message DPA method as mentioned in Section 3.3. Then, we calculate $mask_0$ by $rk_0$ and reveal $wk_0$ with the equation $wk_0 = MASK_0 \oplus mask_0$. Thus, $wk_1, wk_2,$ and $wk_3$ can be revealed by similar procedures. After deriving all the whitening keys, the master key $K$ can be easily derived since $K = wk_0 || wk_1 || wk_2 || wk_3$.

We preset the master key $K$ as four consecutive 32-bit words denoted in hex form, FFEEDDCC-BAAB9988-77665544-33221100, in our FPGA implementation with the loop architecture. Thus, it is obvious that $wk_0 = FFEEDDCC$ and $rk_0 = F3E6CEF9$. We use the attack result of the first Sbox (i.e., $rk_{0,[1]}$ and $MASK_{1,[1]}$) as an example. In Fig.9(a), there are two max points F3D4 and F32B whose correlation coefficients are 0.0743 and −0.0743 respectively. According to the knowledge of the FPGA platform, the power consumption of the FPGA platform has a negative correlation with the Hamming distance power model. Thus, F32B is the attack result (i.e., $rk_{0,[1]} = F3$ and $MASK_{1,[1]} = 2B$), which is revealed within 10000 power traces as shown in Fig.9(b).

We repeat the above procedure 3 times more, and all bytes of $rk_0$ and $MASK_1$ are revealed as $rk_0 = F3E6CEF9$ and $MASK_1 = 2BF18258$. Thus, the value of $mask_1$ is D41F5F94, which is calculated by the round key $rk_0$. And the $wk_0$ is FFEEDDCC, calculated by $mask_1 \oplus MASK_1$. The remaining parts of whitening keys are calculated by similar way. Now, we calculate $K$ is FFEEDDCC-BAAB9988-77665544-33221100, which is identical with the preset master key.

### 4.2 Application to Camellia-128

**Specification of Camellia-128.** Camellia-128, proposed at SAC 2000 by Aoki et al. [3], was jointly designed by NTT and Mitsubishi Electric Corporation. It is widely acknowledged and recommended by ISO [21], NESSIE [22], and
The Negative Peak

The Positive Peak

X-axis: Guessed Parameter $(r_{k_0}/|\text{MASK}_{1,0})^{-10^7}$

Y-axis: Correlation Coefficient

(a)

X-axis: Number of Measurements

Y-axis: Correlation Coefficient

(b)

Fig. 9. Correlation traces in different hypothesis and different number of measurements on CLEFIA

CRYPTREC [23]. It encrypts a 128-bit plaintext into a 128-bit ciphertext with a 128-bit master key after applying the round function 18 times, as shown in Fig.10.

Let $P$ and $K$ be a 128-bit plaintext and a secret key, respectively. Eighteen 64-bit round keys $r_k_1, r_k_2, \cdots, r_k_18$ and four 64-bit whitening keys $w_k_1, w_k_2, w_k_3, w_k_4$ are generated from $K$. Let $L_r$ and $R_r$ ($0 \leq r \leq 18$) be left and right 64-bit of the internal state in each round. According to the key schedule, the pre-whitening keys are defined as $w_{k_1}||w_{k_2} = K$. We omit the descriptions of the $FL$ and $FL^{-1}$ layers after the 6th and 12th rounds, since they have no impacts on our work.

Fig. 10. Camellia encryption algorithm for (a) First two rounds (b) Last two rounds
The round function consists of a 64-bit subkey addition, Sbox transformation, and a diffusion layer called $P$-layer, as shown in Fig.11. Eight parallel 8-bit Sboxes are applied, followed with the $P$-layer which operates on a 64-bit value ($z_1||z_2||\cdots||z_8$). The corresponding output ($z'_1||z'_2||\cdots||z'_8$) is computed as follows.

$$z'_1 = z[1, 3, 4, 6, 7, 8]$$
$$z'_2 = z[1, 2, 4, 5, 7, 8]$$
$$z'_3 = z[1, 2, 3, 5, 6, 8]$$
$$z'_4 = z[2, 3, 4, 5, 6, 7]$$
$$z'_5 = z[1, 2, 6, 7, 8]$$
$$z'_6 = z[2, 3, 5, 7, 8]$$
$$z'_7 = z[3, 4, 5, 6, 8]$$
$$z'_8 = z[1, 4, 5, 6, 7]$$

Here, $z[s, t, u, \cdots]$ means $z_s \oplus z_t \oplus z_u \oplus \cdots$

**Attack of Camellia-128.** Camellia is a Feistel-SP cipher but its $P$-layer does not satisfy the maximum branch number. It has the key whitening layer and the whole plaintext is XORed with the whitening key. Our aim is to reveal the master keys through the recovery of the whitening keys.

We use the notations $L_i$ and $R_i$ for Camellia-128 to represent the state immediately after the round operation in the $i^{th}$ round, especially $L_0$ and $R_0$ to represent the output of the whitening layer before the first round, respectively. We use the notations $PL$ and $PR$ to differentiate the left and right of plaintext, and $S_1$, $S_2$, $S_3$, $S_4$, and $M$ to further distinguish the different Sboxes and diffusion operation of Camellia-128. The subscript $[n]$ indicates the $n^{th}$ byte of the state.

Camellia-128 belongs to the case of whitening keys on both branches. To reveal the master key $K$ of Camellia-128, we focus on two 64-bit pre-whitening key $wk_1$ and $wk_2$, which are defined as $wk_1||wk_2 = K$. The two whitening keys are XORed with two plaintext blocks $PL$ and $PR$ respectively, before the first round. Hence, our attack target is the first two rounds of Camellia-128. According to the attack procedure in the first round of Camellia-128 which is similar to
that of CLEFIA-128, thus we only describe the detailed process to recover \( w_k_1 \) in the second round.

Now, we show how to recover the whitening keys \( w_k_1 \) by attacking the round function \( F \) of the second round. The whitening keys \( w_k_1 \) and \( w_k_2 \) are parallel XORed with two 64-bit plaintext blocks \( PL \) and \( PR \) respectively, and \( r_k_1 \) and \( r_k_2 \) is the round keys as shown in Fig.10. The equivalent key \( e_k_1 \) and the whitening key \( w_k_2 \) are recovered in the first round by the attack process. Therefore, we focus on the second round.

According to the specification of Camellia-128 and Equation.1, the 64-bit output \( L_2 \) is described by

\[
L_2 = F(L_1, r_k_2) \oplus R_1
\]

\[
= M(S_1(L_1, r_k_2) \oplus r_k_2, \oplus w_k_1, \oplus PL,)
\]

\[
= \cdots S_1(L_1, r_k_2) \oplus w_k_1, \oplus PL.
\]  

(11)

Focusing on the first byte of \( L_2 \), Equation.11 could be rewritten as

\[
L_2, [1] = S_1(L_1, r_k_2) \oplus w_k_1, \oplus PL, \oplus \cdot \cdot \cdot 
\]

\[
= S_1(L_1, r_k_2) \oplus w_k_1, \oplus PL, \oplus \cdot \cdot \cdot M_A S K_2, [1] \oplus PL.[1].
\]

(12)

where \( mask_2, [1] \) is generated by \( S_2(L_1, r_k_2) \), \( S_3(L_1, r_k_2) \), \( \cdots \), \( S_1(L_1, r_k_2) \) and \( M_A S K_2 \) is defined as \( M_A S K_2 = mask_2 \oplus w_k_1 \).

Before launch attack in the second round, we should calculate the corresponding plaintext message with \( e_k_1 \) and \( w_k_2 \) through the inverse transformation of Camellia round function, according to the value of \( L_1 \) which meets the chosen message requirements. Fortunately, we find that there is an one-to-one mapping relationship between \( PR \) and \( L_1 \). Thus, we can control \( L_2 \) by enumerating \( PR \), and reveal the value \( w_k_1 \) by the method as mentioned in Section 3.4. After deriving all the whitening keys, the master key \( K \) can be easily derived since

\[
K = w_k_1||w_k_2.
\]

We preset the master key \( K \) as four consecutive 32-bit words denoted in hex form, \( 01234567-89ABCDEF-FEDCBA98-76543210 \), in our FPGA implementation with the loop architecture. Thus, it is obvious that \( w_k_1 = 01234567-89ABCDEF \).

We use the attack result of the third Sbox (i.e., \( r_k_2, [3] \) and \( M_A S K_2, [3] \)) as an example. In Fig.12(a), there are two max points \( 40B8 \) and \( 4047 \) whose correlation coefficients are 0.107 and -0.107 respectively. According to the negative correlation between the power consumption of the FPGA platform and the Hamming distance power model, \( 4047 \) is the attack result (i.e., \( r_k_2, [3] = 40 \) and \( M_A S K_2, [3] = 47 \)), which is revealed within 4000 power traces as shown in Fig.12(b).

5 Conclusion

In this paper, we propose a practical chosen message power analysis method on loop architecture of ciphers with the key whitening layers. Then we apply our
method to CLEFIA-128 and Camellia-128, and the master keys are recovered as expected. Following the results presented in this work, several problems which are worth further investigations emerge:

- **Optimizations.** The first natural question emerges is whether our method can be further optimized. One possible direction of improvement is taking advantage of more powerful DPA method, such as the adaptive strategy in [7, 17] and the multiple CPA in [15], to discriminate the correct hypothesis from the key candidates in a more efficient way. Other potential optimizations are also possible directions for future research.

- **Countermeasures.** Next to optimality, another important question is to determine the countermeasures against such attack. Our method is suitable for the unprotected loop hardware implementations. Several common countermeasures on the compact architecture [18], can be considered to apply to the loop architecture in order to resist our approach, while the resource consumption will have a corresponding increase. Moreover, the countermeasures based on the mask methodology should be used with caution on the loop implementations of ciphers, because the mask countermeasures usually lead to slow computation speed. Considering the limitation of high computation speed and high throughput in the application scenario, the loop implementations of ciphers must keep the high performance, when the countermeasures against such attack are applied on these implementations. Thus, a trade-off between performance and security should be considered by the vendor.

References


